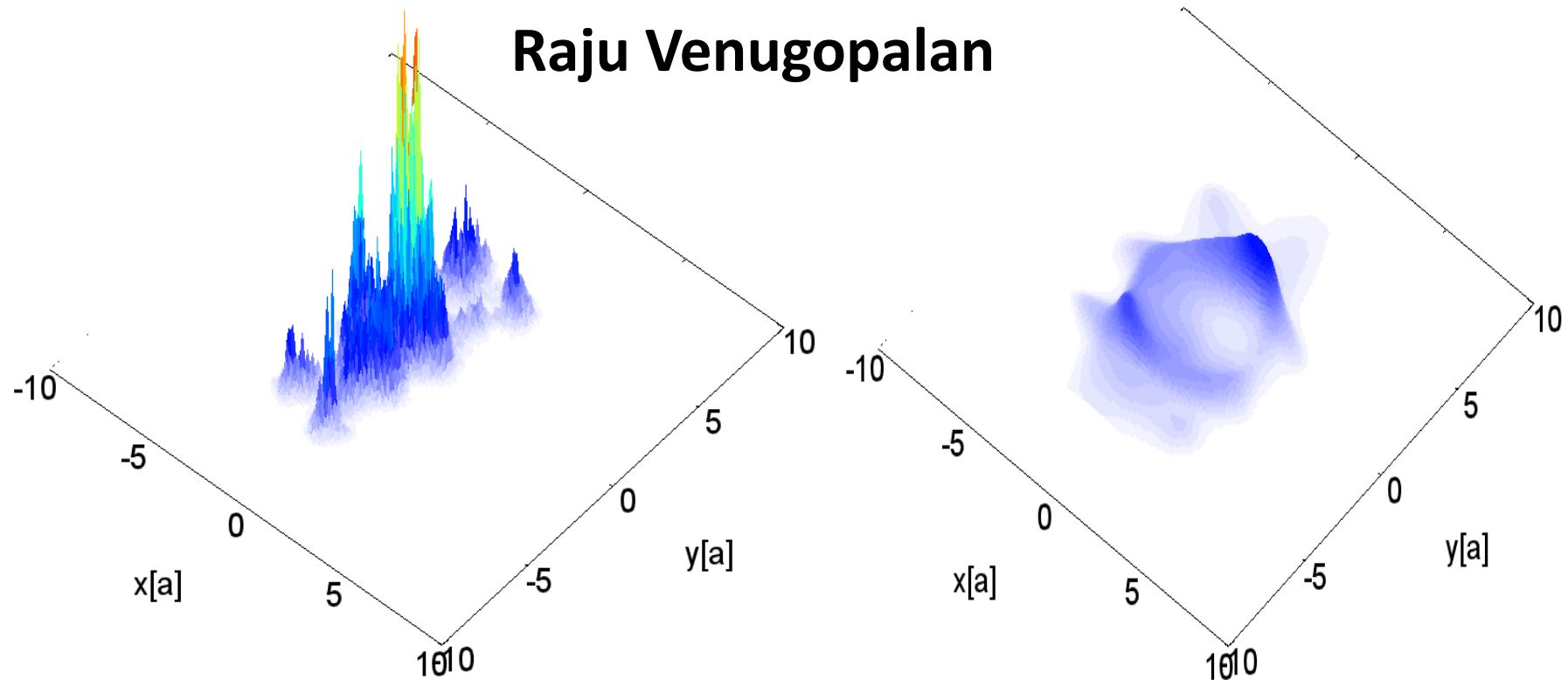


The Glasma: coherence, evolution, correlations

Raju Venugopalan



Lecture II, JET school, June 2012

Outline of lectures

- ◆ **Lecture I: Gluon Saturation and the Color Glass Condensate**
- ◆ **Lecture II: Quantum field theory in strong fields. Factorization. the Glasma and long range correlations**
- ◆ **Lecture III: Quantum field theory in strong fields. Instabilities, spectrum of initial quantum fluctuations, decoherence, hydrodynamics, B-Einstein condensation & thermalization**

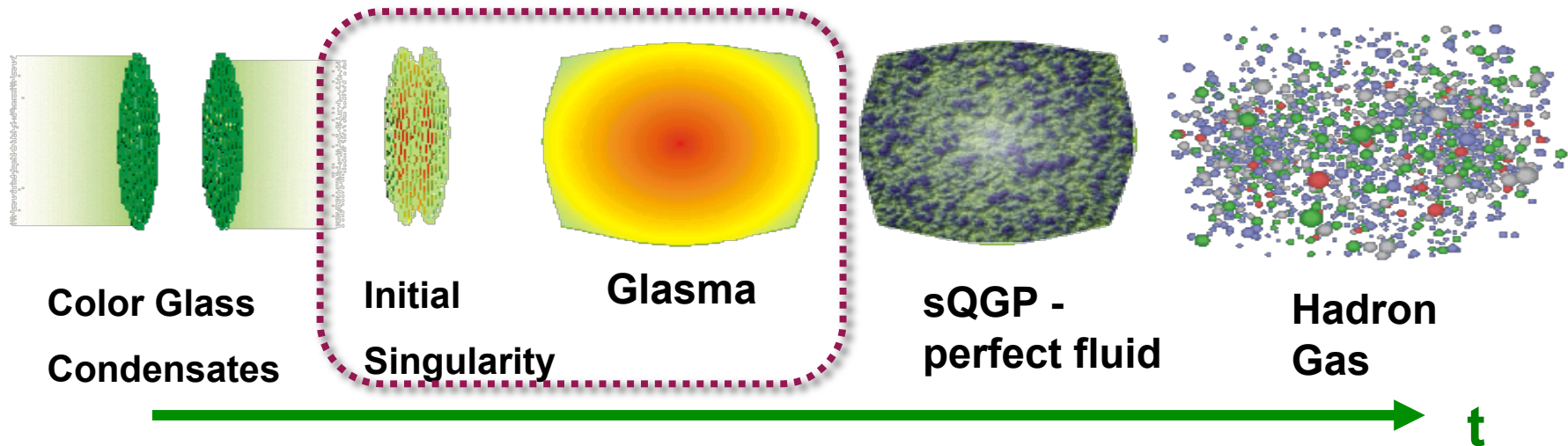
Traditional picture of heavy ion collisions



***@\$#! on *@\$#!**

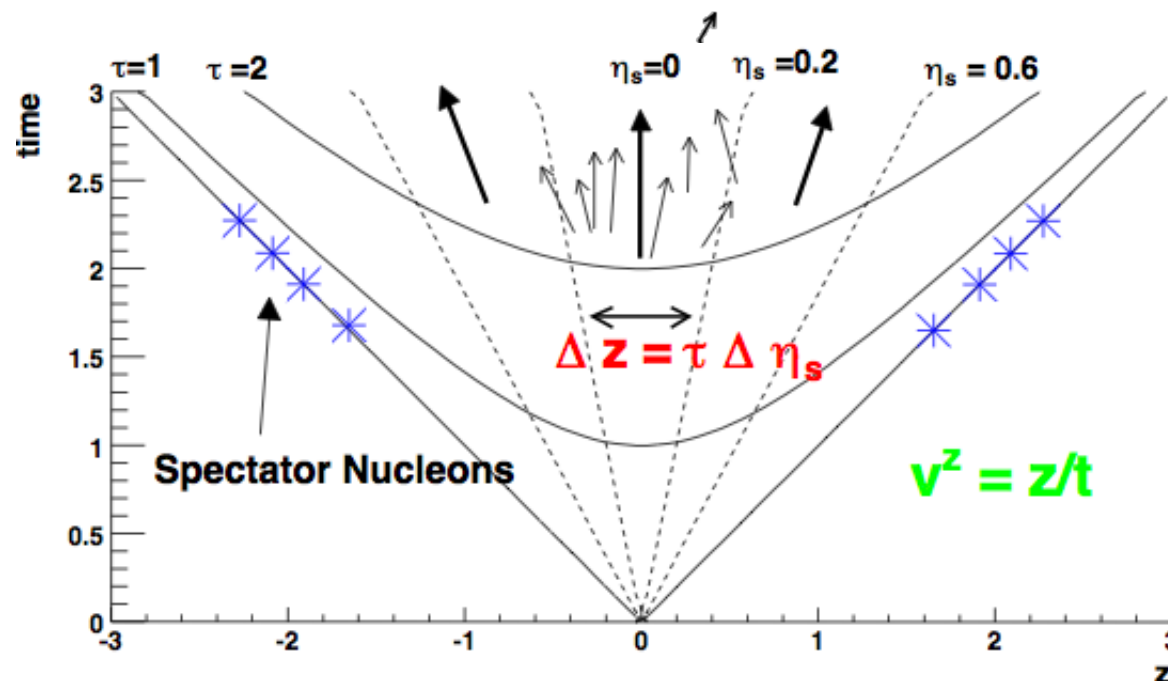
Well known physicist (circa early 1980s)

Standard model of HI Collisions



Glasma (\Glahs-maa\): *Noun*: non-equilibrium matter between Color Glass Condensate (CGC) & Quark Gluon Plasma (QGP)

Forming a Glasma in the little Bang

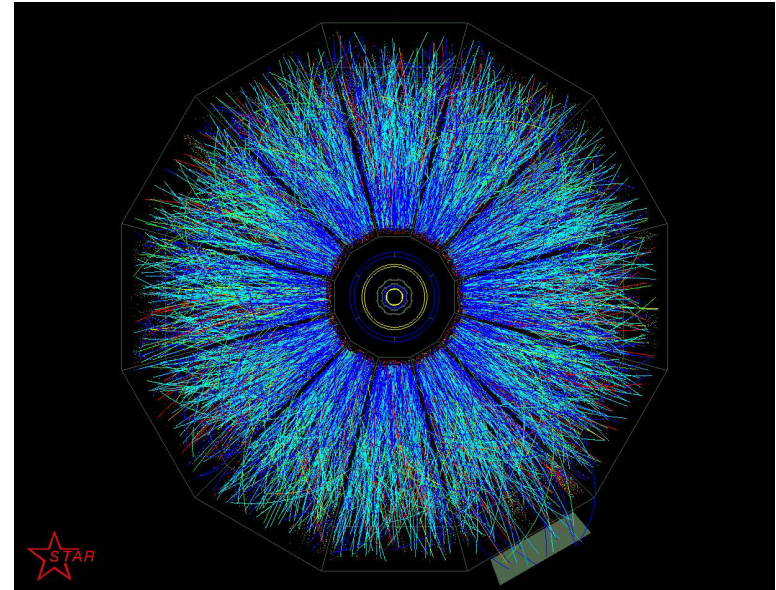


- ❖ Problem: Compute particle production in QCD with *strong time dependent* sources
- ❖ Solution: for early times ($t \leq 1/Q_s$) -- n-gluon production computed in A+A to all orders in pert. theory to leading log accuracy

Gelis, Lappi, RV; arXiv : 0804.2630, 0807.1306, 0810.4829

THE LITTLE BANG

How can we compute multiparticle production *ab initio* in HI collisions ?



~~-perturbative VS non-perturbative,~~

strong coupling VS weak coupling

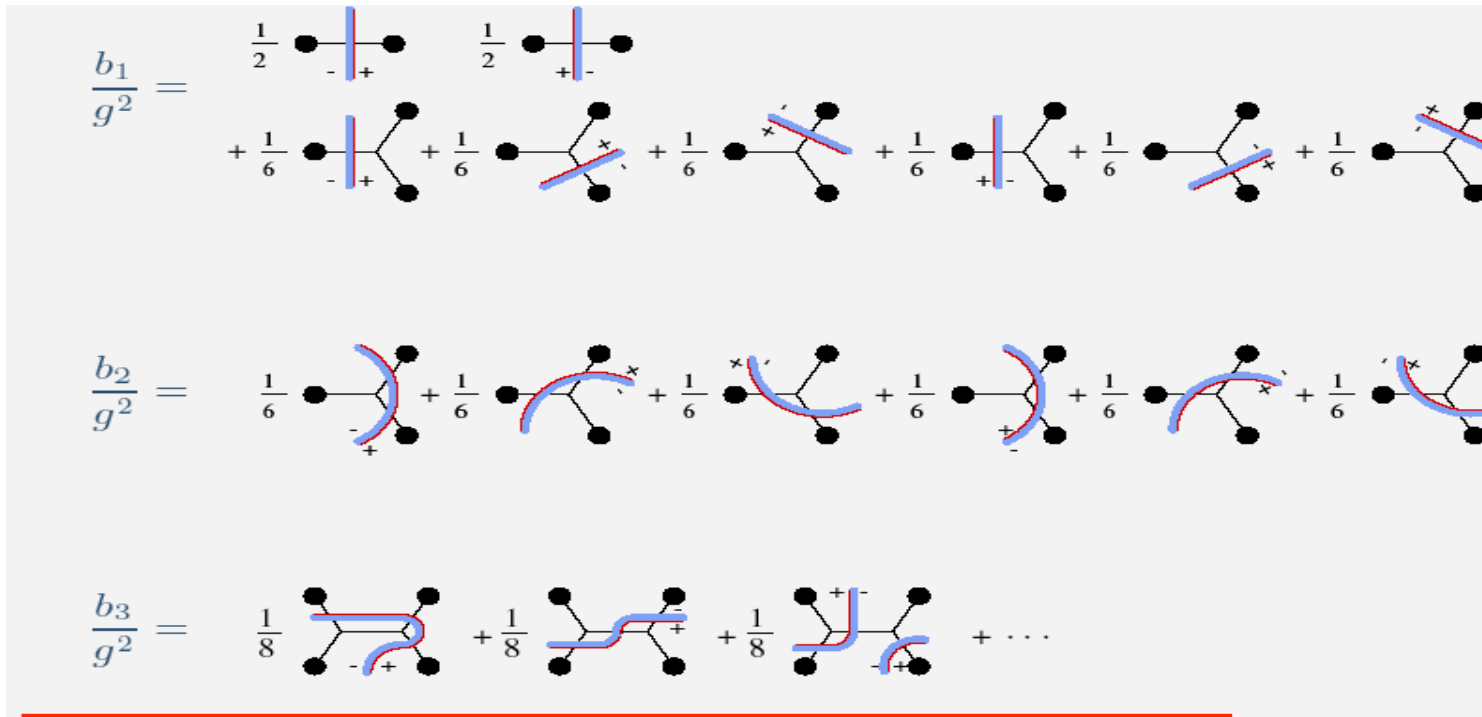


AdS/CFT ? Interesting set of issues... not discussed here

Always non-perturbative
for questions of
interest in this talk!

Multiparticle production for strong time dependent sources:

Gelis, RV ; NPA776 (2006)



$$P_n = e^{-\frac{1}{g^2} \sum_r b_r} \sum_{p=1}^n \frac{1}{p!} \sum_{\alpha_1 + \dots + \alpha_p = n} \frac{b_{\alpha_1} \dots b_{\alpha_p}}{g^{2p}}$$

b_r - probability of vacuum-vacuum diagrams with r cuts

“combinants”

Observations:

- I) P_n is **non-perturbative** for any n
and for coupling $g \ll 1$ - no simple power counting in g
- II) Even at tree level, P_n is *not a Poisson dist.*
- III) *However, vacuum-vacuum contributions cancel for inclusive quantities*
($\langle n^p \rangle = \Sigma n^p P_n / \Sigma P_n$)
and one has systematic power counting for these...

Power counting

LO: $1/g^2$, all orders in sources $(g\rho_{1,2})^n$

NLO: $O(1)$, all orders in $(g\rho_{1,2})^n$

At NLO, large logs : $g^2 \ln(1/x_{1,2})$ – can be resummed to all orders and factorized
into evolution of wave functions

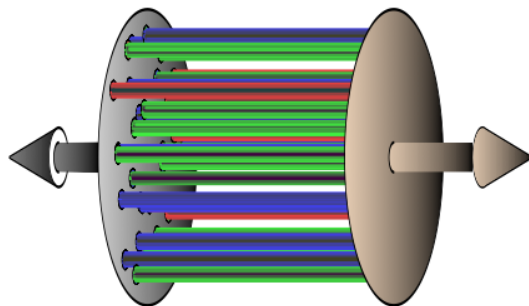
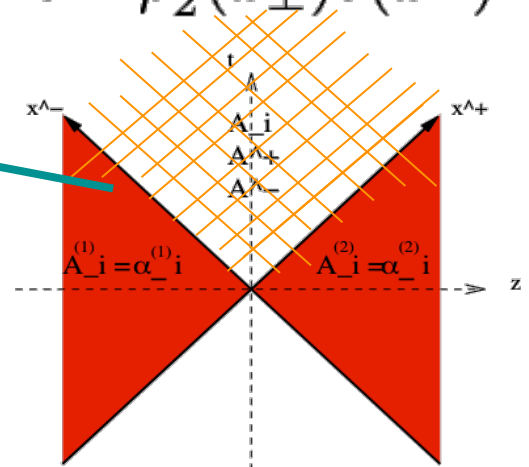
The Glasma at LO: Yang-Mills eqns. for two nuclei

$O(1/g^2)$ and all orders in $(g\rho)^n$

$$D_\mu F^{\mu\nu,a} = \delta^{\nu+} \rho_1^a(x_\perp) \delta(x^-) + \delta^{\nu-} \rho_2^a(x_\perp) \delta(x^+)$$

Glasma initial conditions from matching classical **CGC** wave-fns on light cone

Kovner, McLerran, Weigert; Krasnitz, RV; Lappi
Lappi, Srednyak, RV (2010)



$$\begin{aligned} \nabla \cdot E &= \rho_{\text{electric}} \\ \nabla \cdot B &= \rho_{\text{magnetic}} \end{aligned}$$

$$\begin{aligned} \rho_{\text{electric}} &= ig[A^i, E^i] \\ \rho_{\text{magnetic}} &= ig[A^i, B^i] \end{aligned}$$

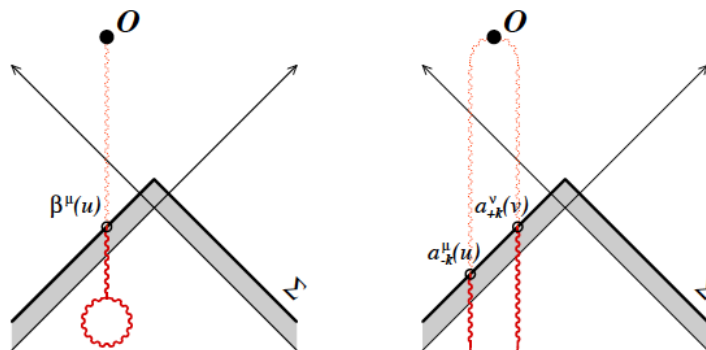
Boost invariant flux tubes of size with $||$ color E & B fields- generate Chern-Simons charge

However, this results in very anisotropic ($P_T \gg P_L$) pressure for $\tau \sim 1/Q_s$

RG evolution for 2 nuclei

Gelis,Lappi,RV (2008)

Log divergent contributions crossing nucleus 1 or 2:



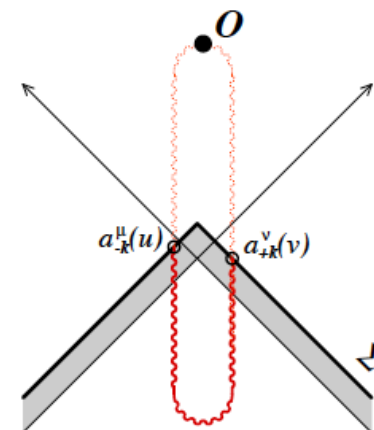
$$\mathcal{O}_{\text{NLO}} = \left[\frac{1}{2} \int_{\vec{u}, \vec{v}} \mathcal{G}(\vec{u}, \vec{v}) \mathcal{T}_u \mathcal{T}_v + \int_{\vec{u}} \beta(\vec{u}) \mathcal{T}_u \right] \mathcal{O}_{\text{LO}}$$

$\mathcal{G}(\vec{u}, \vec{v})$ and $\beta(\vec{u})$ can be computed on the initial Cauchy surface

$$\mathcal{T}_u = \frac{\delta}{\delta A(\vec{u})} \quad \text{linear operator on initial surface}$$

Contributions across both nuclei are finite-no log divergences => factorization

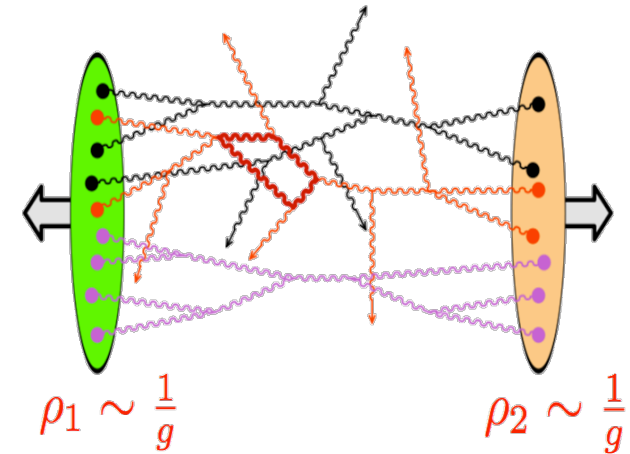
$$\mathcal{O}_{\text{NLO}} = \left[\ln \left(\frac{\Lambda^+}{p^+} \right) \mathcal{H}_1 + \ln \left(\frac{\Lambda^-}{p^-} \right) \mathcal{H}_2 \right] \mathcal{O}_{\text{LO}}$$



Factorization + temporal evolution in the Glasma

$$T_{\text{LO}}^{\mu\nu} = \frac{1}{4} g^{\mu\nu} F^{\lambda\delta} F_{\lambda\delta} - F^{\mu\lambda} F_{\lambda}^{\nu} \quad \mathcal{O}\left(\frac{Q_S^4}{g^2}\right)$$

$\epsilon = 20\text{-}40 \text{ GeV/fm}^3$ for $\tau = 0.3 \text{ fm}$ @ RHIC



**NLO terms are as large as LO for $\alpha_s \ln(1/x)$:
small x (leading logs) and strong field (gp) resummation**

Gelis, Lappi, RV (2008)

$$\langle T^{\mu\nu}(\tau, \underline{\eta}, x_{\perp}) \rangle_{\text{LLog}} = \int [D\rho_1 d\rho_2] W_{Y_1}[\rho_1] W_{Y_2}[\rho_2] T_{\text{LO}}^{\mu\nu}(\tau, x_{\perp})$$

$Y_1 = Y_{\text{beam}} - \eta; Y_2 = Y_{\text{beam}} + \eta$

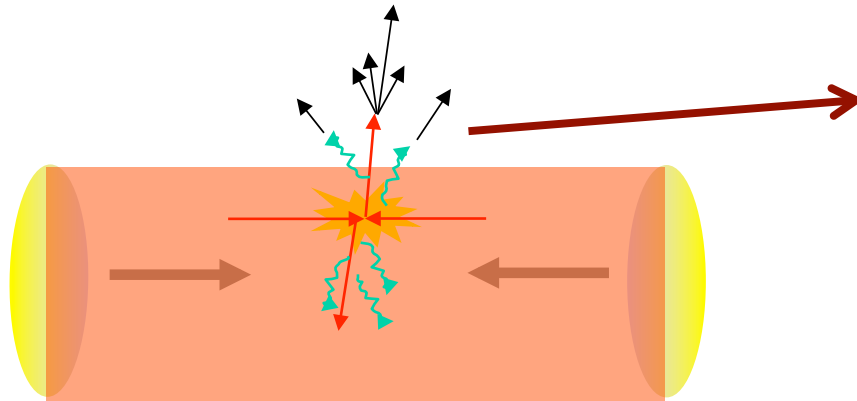
Glasma factorization => universal “density matrices W ” \otimes “matrix element”

Some consequences of the Glasma flux tube picture

- **Compute long range rapidity correlations (the ridge in p+p and A+A)**
- **Compute n-particle distributions, incorporate these along with geometrical fluctuations in event-by-event hydro models**

Long range rapidity correlations

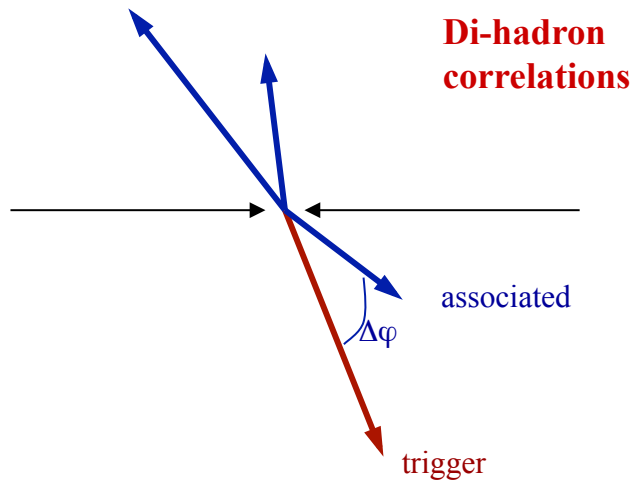
Some notation: $\Delta\eta$ - $\Delta\Phi$



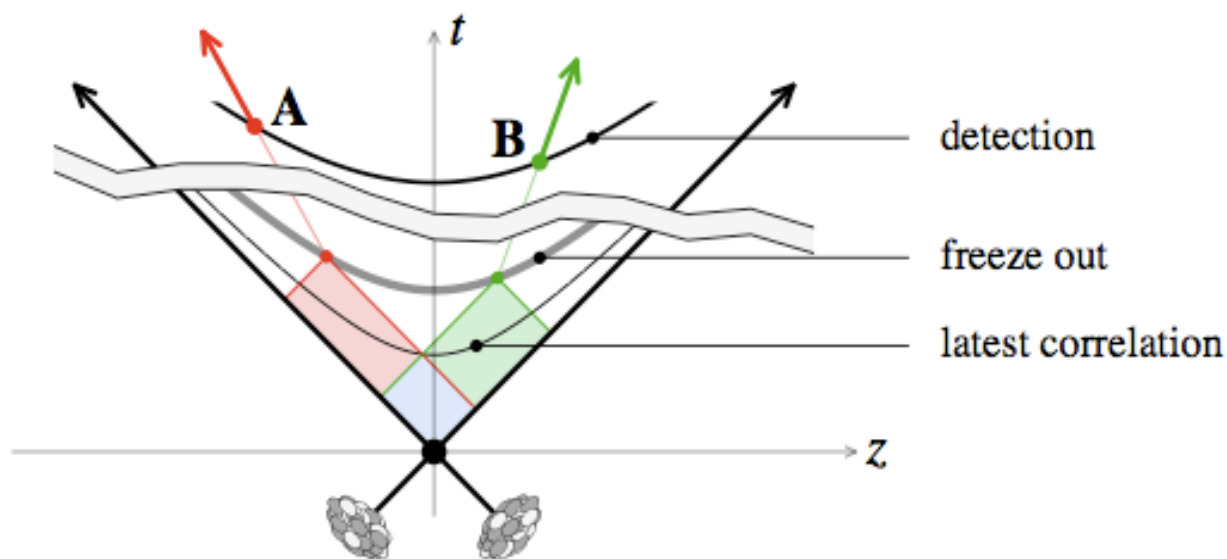
Rapidity: a measure of velocity (denoted by y or η) additive under Lorentz boost

$\Delta\eta$ – measure of angular separation along beam direction

Large $\Delta\eta$ means particles are flying off in opposite directions along beam axis



Long range rapidity correlations as chronometer

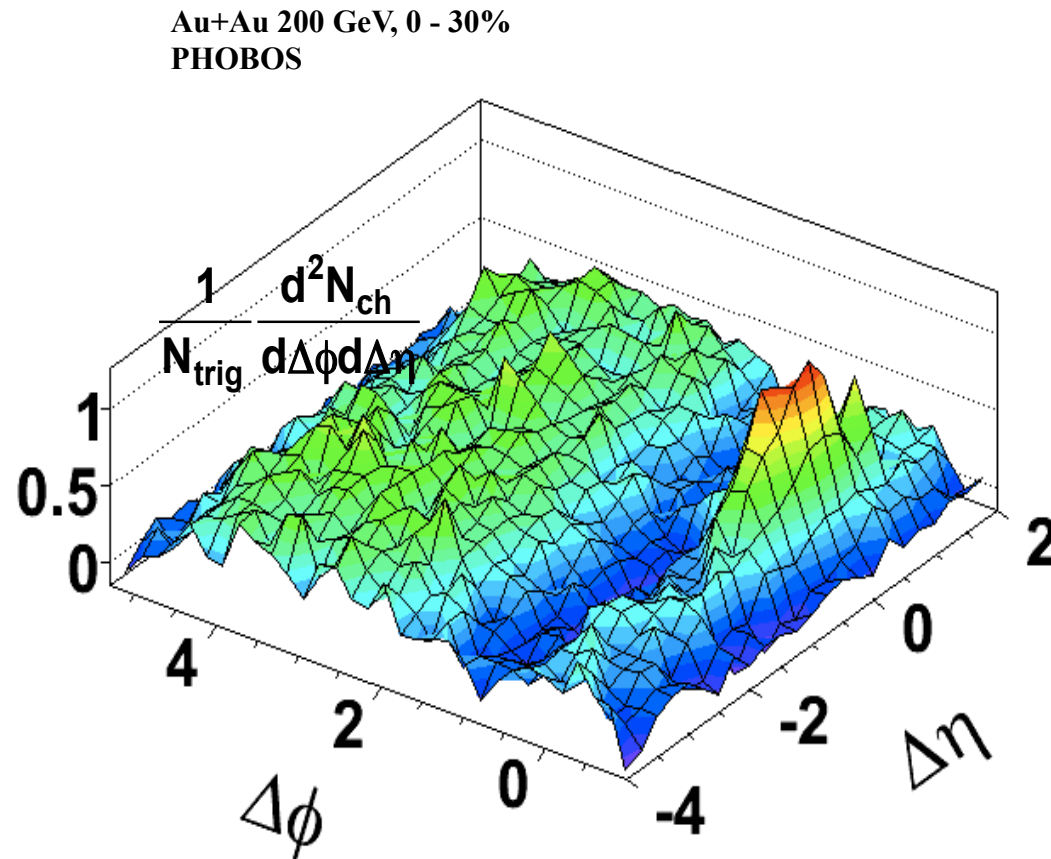


$$\tau \leq \tau_{\text{freeze-out}} \exp\left(-\frac{1}{2}|y_A - y_B|\right)$$

Long range rapidity correlations are sensitive to Glasma dynamics at early times

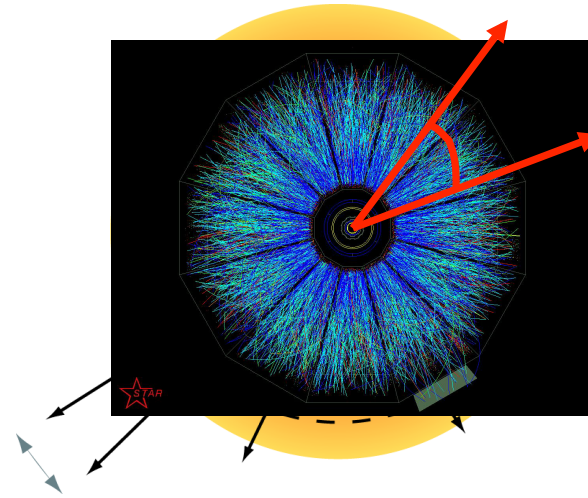
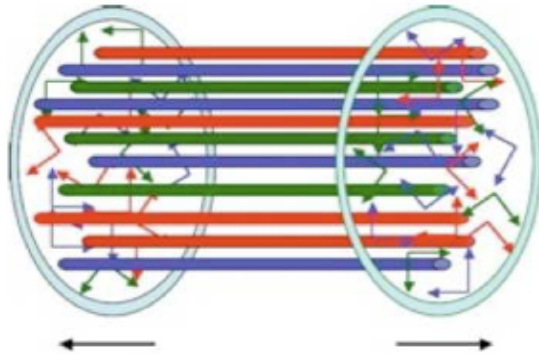
Dumitru, Gelis, McLerran, RV, arXiv 0804.3858

Really long range correlations



These structures reflect dynamics of strong gluon fields at times $< 3 \cdot 10^{-24}$ seconds

The Ridge: Glasma flux tubes+ Radial flow



Glasma flux tubes provide the long range rapidity correlation

Dumitru, Gelis, McLerran, RV; Gavin, McLerran, Moschelli
Lappi, Srednyak, RV (2010)

Radial (“Hubble”) flow of the tubes provides the azimuthal collimation

Voloshin; Shuryak



Particles That Flock: Strange Synchronization Behavior at the Large Hadron Collider

Scientists at the Large Hadron Collider are trying to solve a puzzle of their own making: why particles sometimes fly in sync

Scientific American, February (2011)

The high-energy collisions of protons in the LHC may be uncovering “a new deep internal structure of the initial protons,” says Frank Wilczek of the Massachusetts Institute of Technology, winner of a Nobel Prize

“At these higher energies [of the LHC], one is taking a snapshot of the proton with higher spatial and time resolution than ever before”



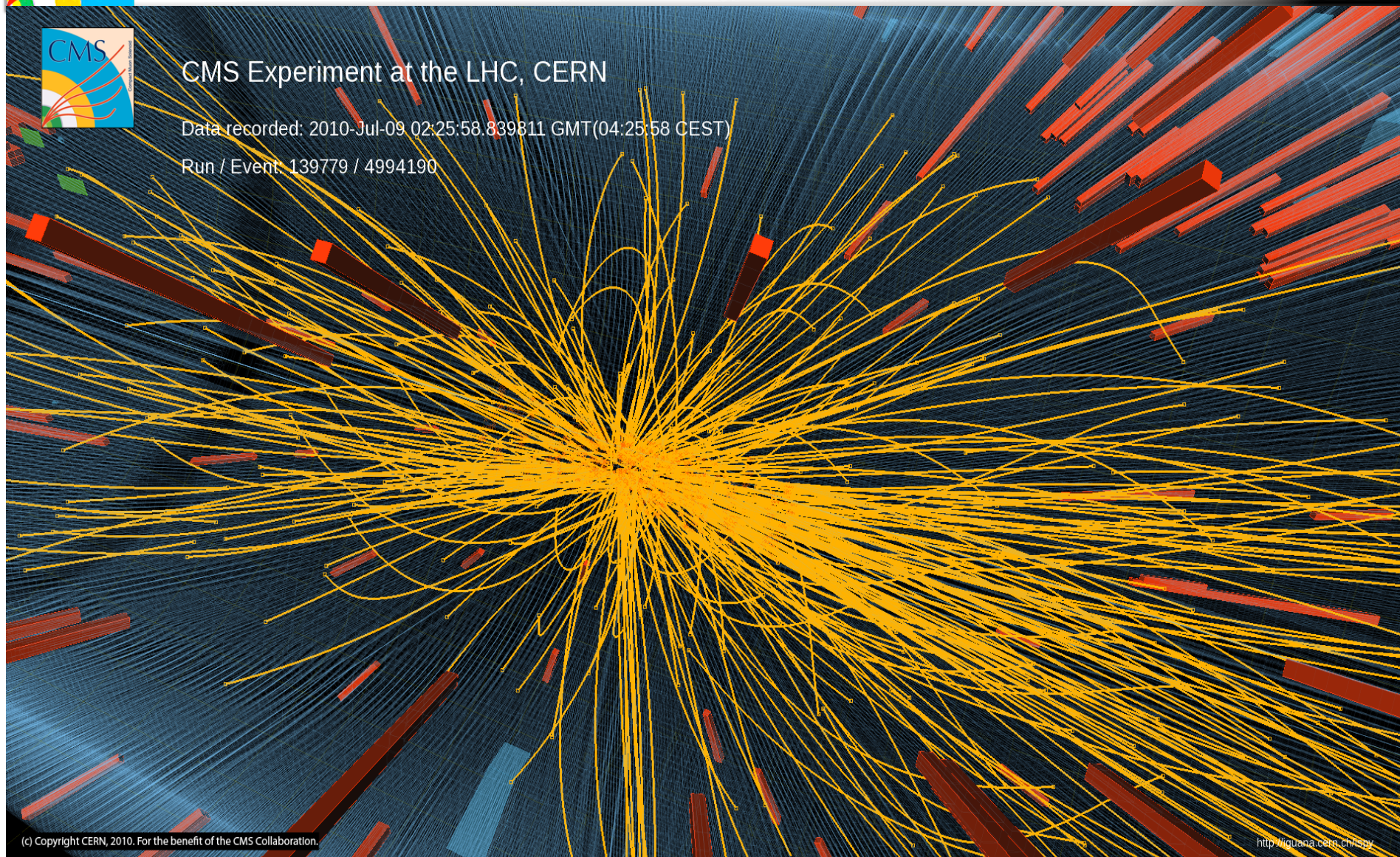
A ridge in high multiplicity pp collisions



CMS Experiment at the LHC, CERN

Data recorded: 2010-Jul-09 02:25:58.839811 GMT(04:25:58 CEST)

Run / Event: 139779 / 4994190



(c) Copyright CERN, 2010. For the benefit of the CMS Collaboration.

<http://lqana.cern.ch/lsby>



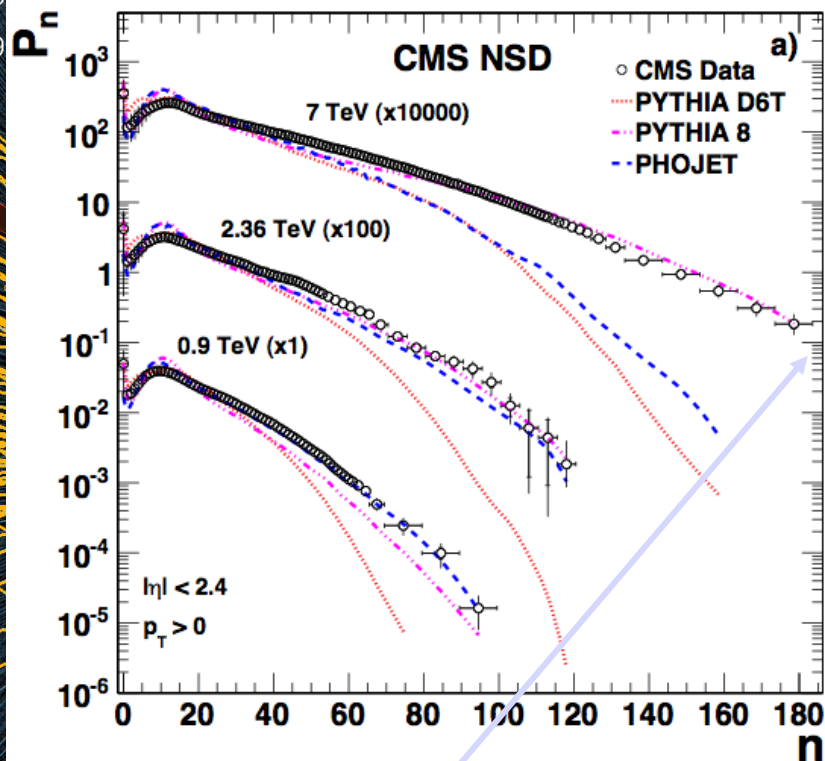
High Multiplicity pp collisions



CMS Experiment High Multiplicity events are rare in nature

Data recorded: 2010-Jul-0

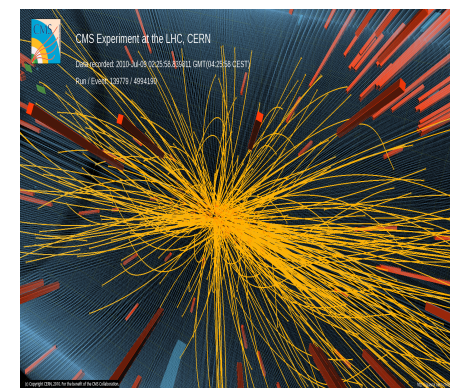
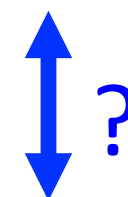
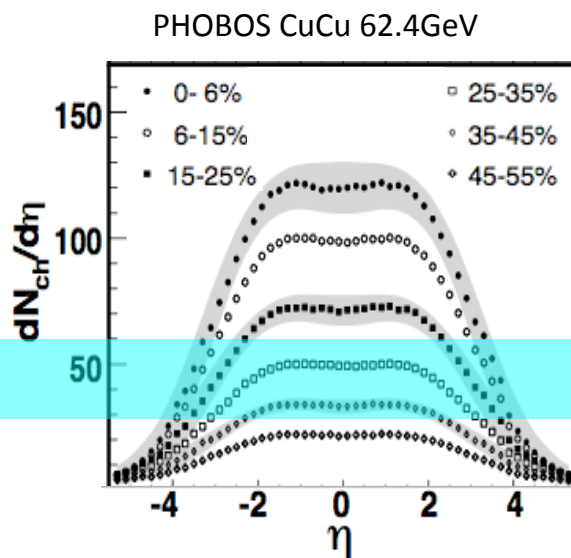
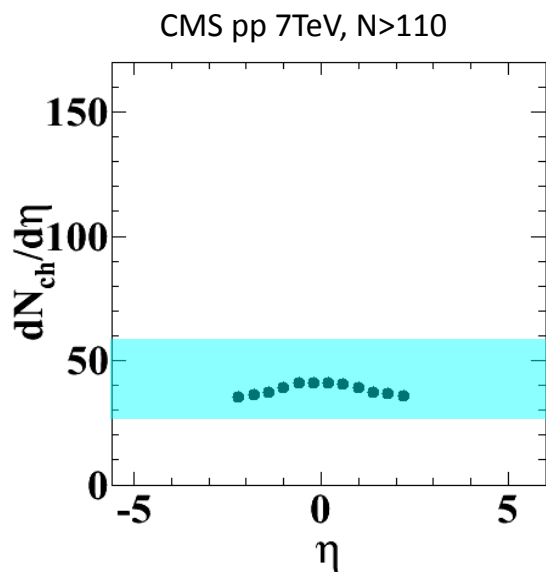
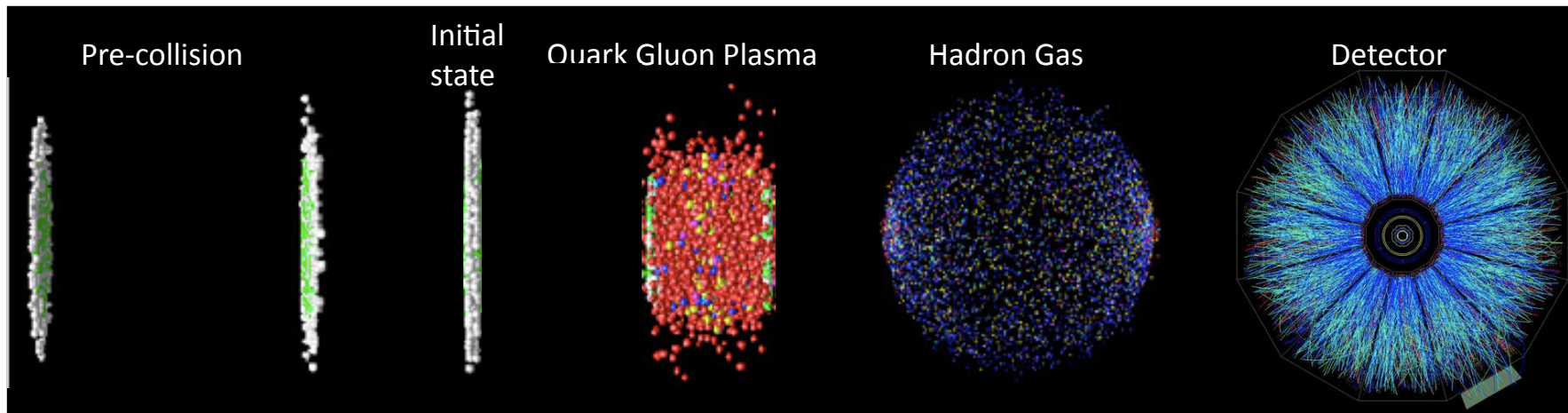
Run / Event: 139779 / 499



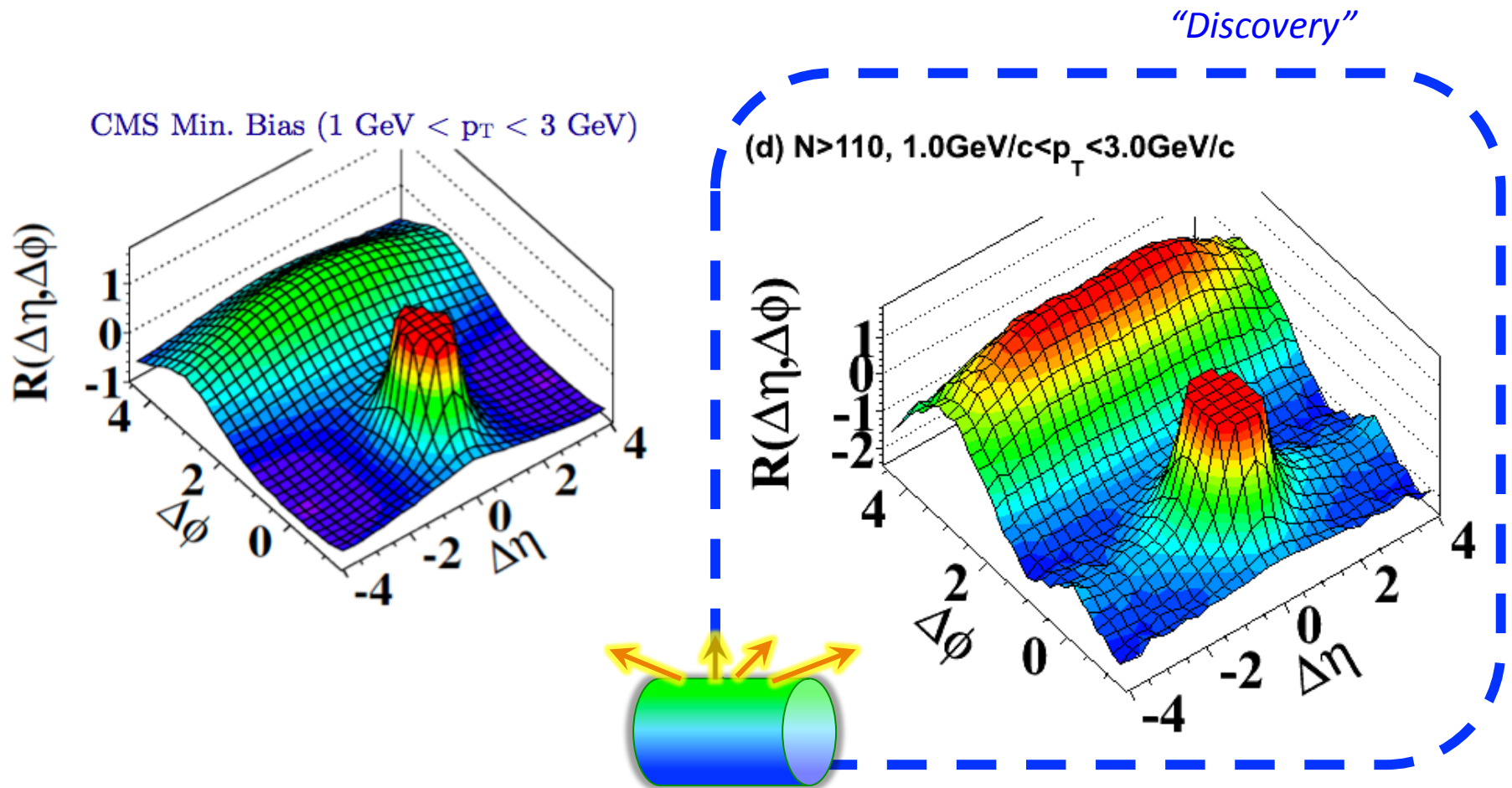
Very high particle density regime
Is there anything peculiar happening there?



Relativistic Heavy Ion Collisions

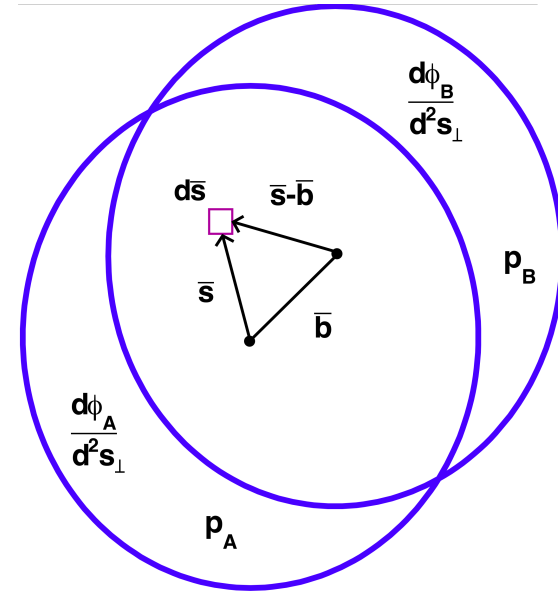
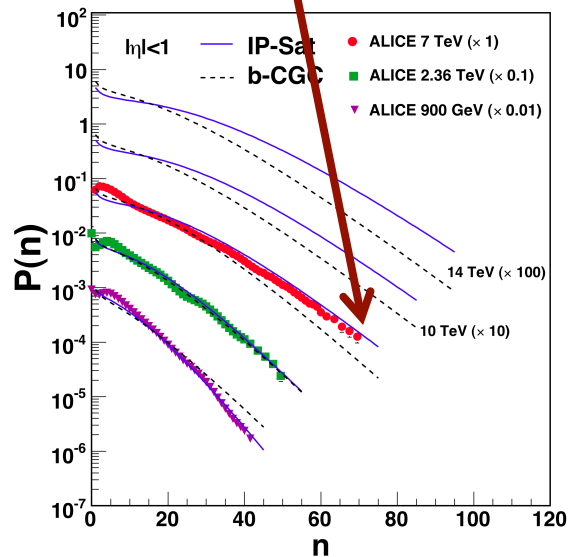
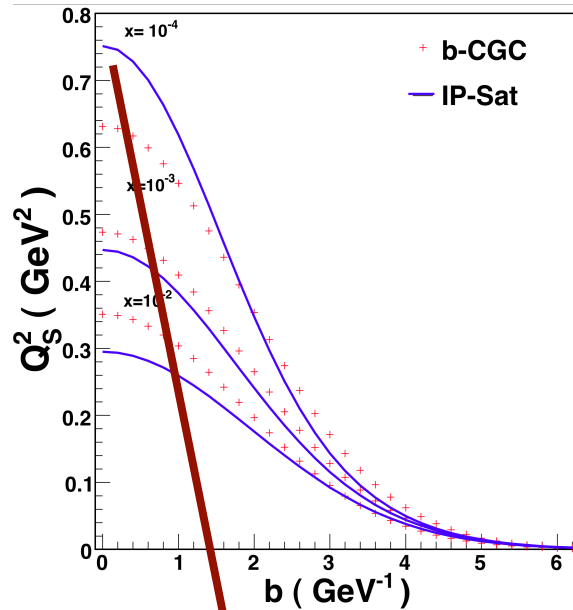


Two particle correlations: CMS results



- ◆ Ridge: Distinct long range correlation in η collimated around $\Delta\Phi \approx 0$ for two hadrons in the intermediate $1 < p_T, q_T < 3 \text{ GeV}$

High multiplicity events in p+p

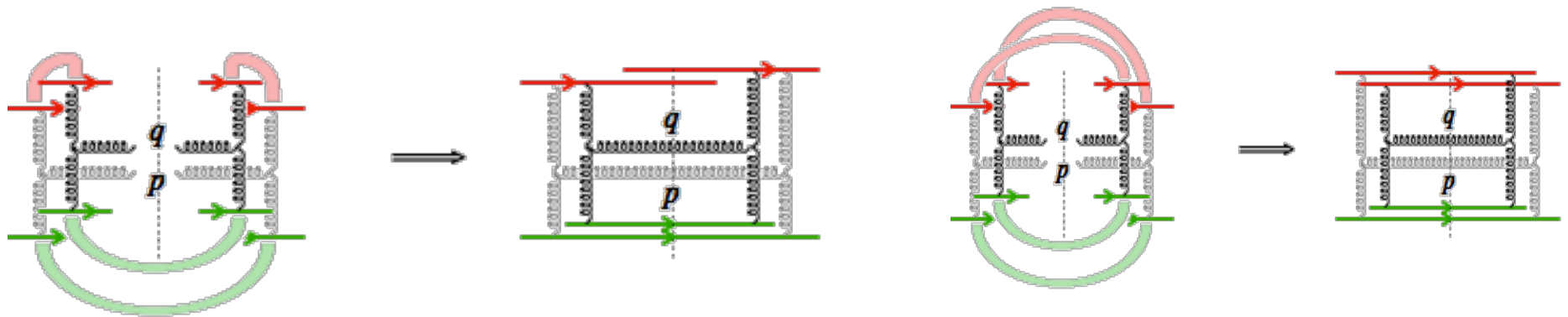


High multiplicity events likely correspond to **high occupation numbers ($1/\alpha_s$)** in the proton wave functions for $p_T \leq Q_s$

I will emphasize this point further shortly

The saturated proton: two particle correlations

Correlations are induced by color fluctuations that vary event to event - these are local transversely and have **color screening radius $\sim 1/Q_s$**



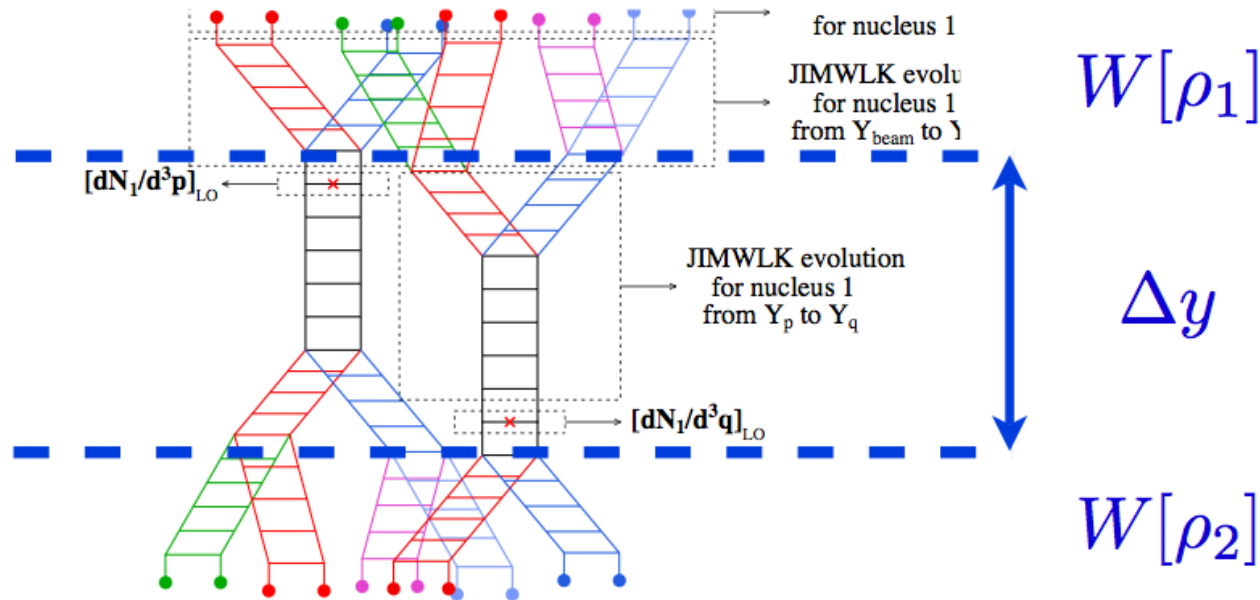
These graphs (called “Glasma graphs”), which generate long range rapidity correlations, are highly suppressed for $Q_s \ll p_T$

However, effective coupling of sources to fields with $k_T \leq Q_s = 1/g$ (“saturation”)

Power counting changes for high multiplicity events by α_s^8 !
These graphs become competitive with usual pQCD graphs

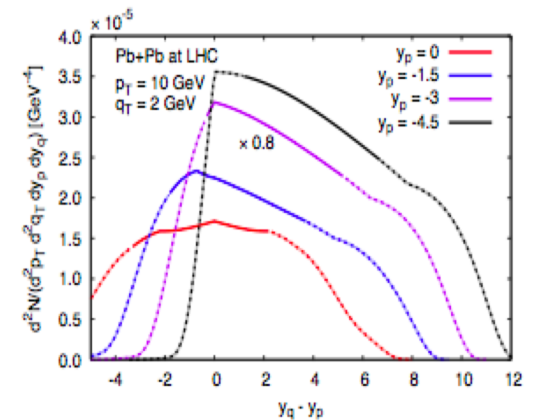
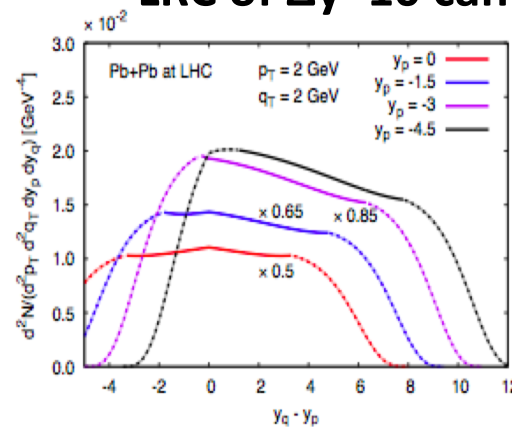
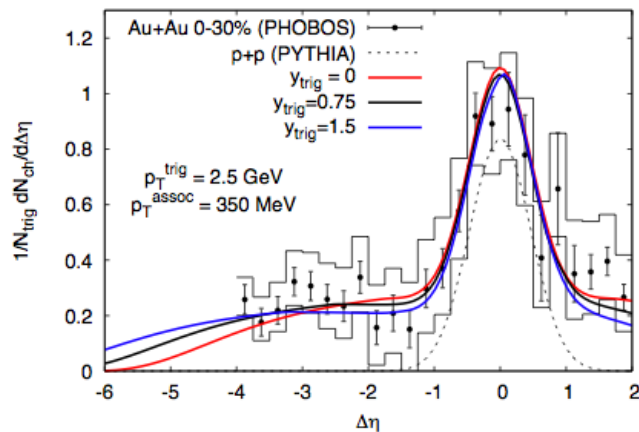
Long range di-hadron correlations

Gelis,Lappi,RV (2009)



Dusling,Gelis,Lappi,RV, arXiv:0911.2720

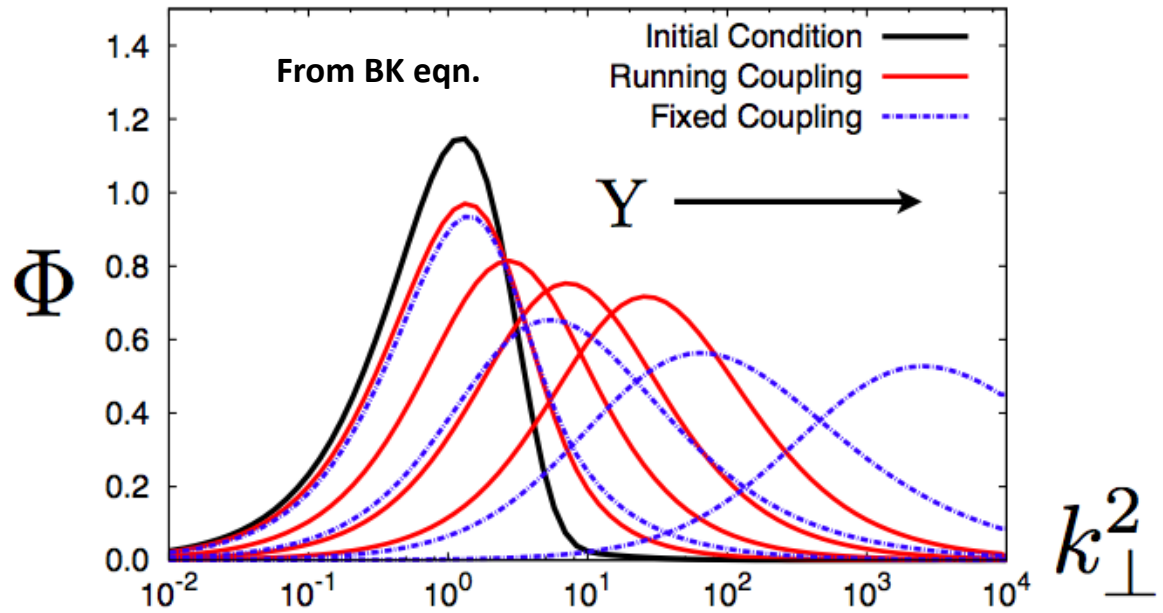
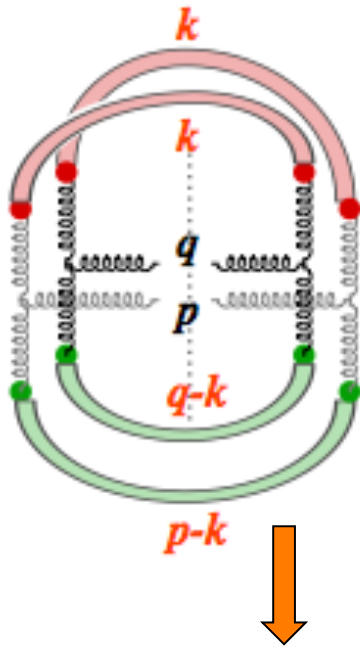
LRC of $\Delta y \sim 10$ can be studied at the LHC



Long range di-hadron correlations

RG evolution of two particle correlations (in mean field approx) expressed in terms of “unintegrated gluon distributions” [Dusling,Gelis,Lappi,RV \(2009\)](#)

$$C(\mathbf{p}, \mathbf{q}) \propto \frac{g^4}{\mathbf{p}_\perp^2 \mathbf{q}_\perp^2} \int d^2 \mathbf{k}_{1\perp} \Phi_{A_1}^2(y_p, \mathbf{k}_{1\perp}) \Phi_{A_2}(y_p, \mathbf{p}_\perp - \mathbf{k}_{1\perp}) \Phi_{A_2}(y_q, \mathbf{q}_\perp - \mathbf{k}_{1\perp}) + \text{permutations}$$



Such “Glasma flux tube” graphs are enhanced by α_s^{-8} at high parton densities...

[Dumitru,Dusling,Gelis,Jalilian-Marian,Lappi,RV, arXiv:1009.5295](#)

Quantitative description of pp ridge

Dusling,RV, 1201.2658

$$\frac{d^2 N}{d\Delta\phi} = K \int_{-2.4}^{+2.4} d\eta_p d\eta_q \mathcal{A}(\eta_p, \eta_q)$$

$$\times \int_{p_T^{\min}}^{p_T^{\max}} \frac{dp_T^2}{2} \int_{q_T^{\min}}^{q_T^{\max}} \frac{dq_T^2}{2} \int d\phi_p \int d\phi_q \delta(\phi_p - \phi_q - \Delta\phi)$$

$$\times \int_0^1 dz_1 dz_2 \frac{D(z_1)}{z_1^2} \frac{D(z_2)}{z_2^2} \frac{d^2 N_{\text{Glasma}}^{\text{corr.}}}{d^2 p_T d^2 q_T d\eta_p d\eta_q} \left(\frac{p_T}{z_1}, \frac{q_T}{z_2}, \Delta\phi \right)$$

$$\mathcal{A}(\eta_p, \eta_q) = \theta(|\eta_p - \eta_q| - \Delta\eta_{\min}) \theta(\Delta\eta_{\max} - |\eta_p - \eta_q|)$$

Try soft and hard fragmentation functions:

$$D_1 = 3(1-x)^2 / x$$

$$D_2 = 2(1-x) / x$$

$$N_{\text{trig}} = \int_{-2.4}^{+2.4} d\eta \int_{p_T^{\min}}^{p_T^{\max}} d^2 p_T \int_0^1 dz \frac{D(z)}{z^2} \frac{dN}{d\eta d^2 p_T} \left(\frac{p_T}{z} \right)$$

Only parameter fit to yield data is $K = 2.3$

$$\text{Assoc. Yield} = \frac{1}{N_{\text{trig}}} \int_0^{\Delta\phi_{\min.}} d\Delta\phi \frac{d^2 N}{d\Delta\phi} - \left. \frac{d^2 N}{d\Delta\phi} \right|_{\Delta\phi_{\min.}}$$

Dependence on transverse area cancels in ratio...

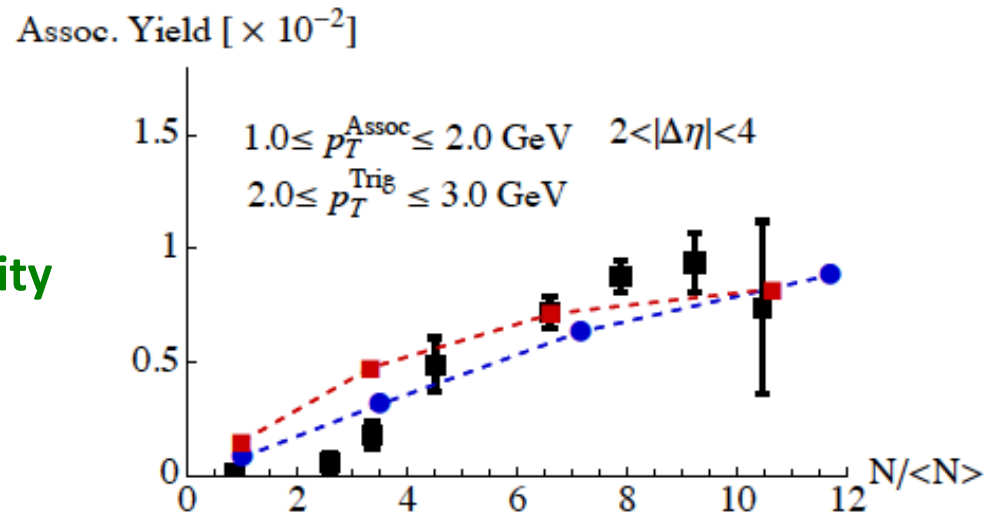
Subtracts any pedestal “phi-independent” correlation

Quantitative description of pp ridge

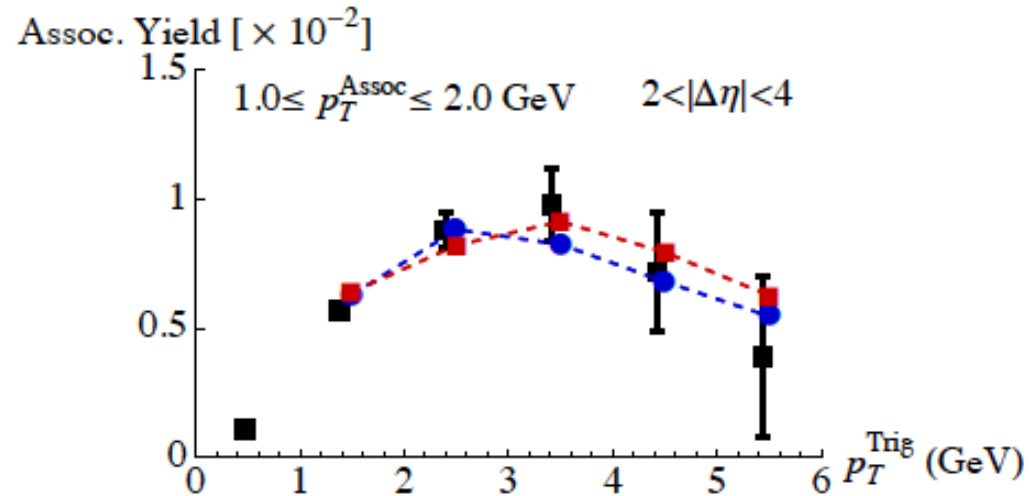
Dusling, RV, 1201.2658, PRL, in press

CMS preliminary data

Assoc. yield with centrality



Assoc. yield with p_T^{Trig}

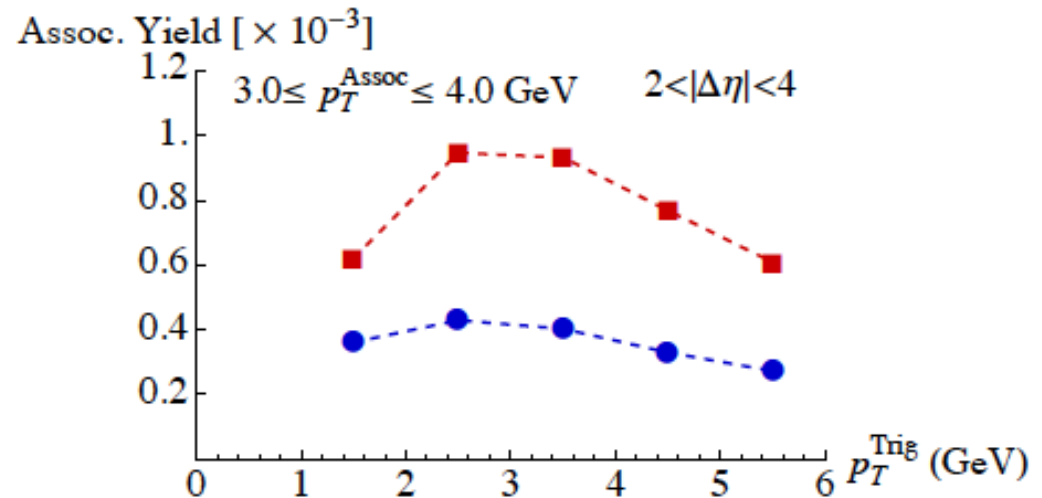
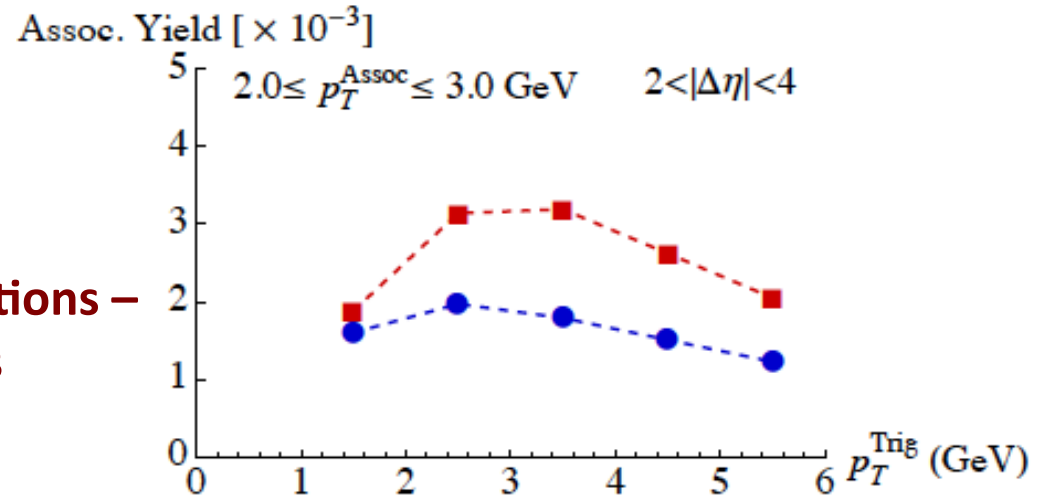


Quantitative description of pp ridge

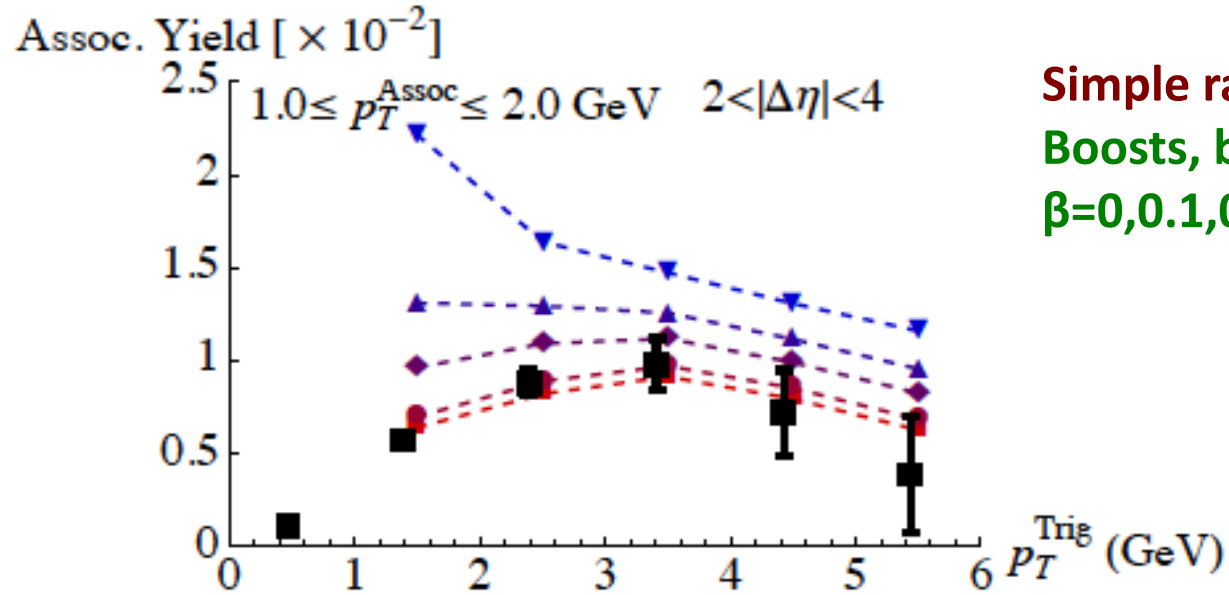
Dusling,RV, 1201.2658

Predictions:

Yields for higher $p_T^{\text{Assoc.}}$ are sensitive to fragmentation functions – not known at forward rapidities



What about flow in p+p ?



Simple radial flow model result:

Boosts, bottom to top,

$\beta=0,0.1,0.2,0.25,0.3$

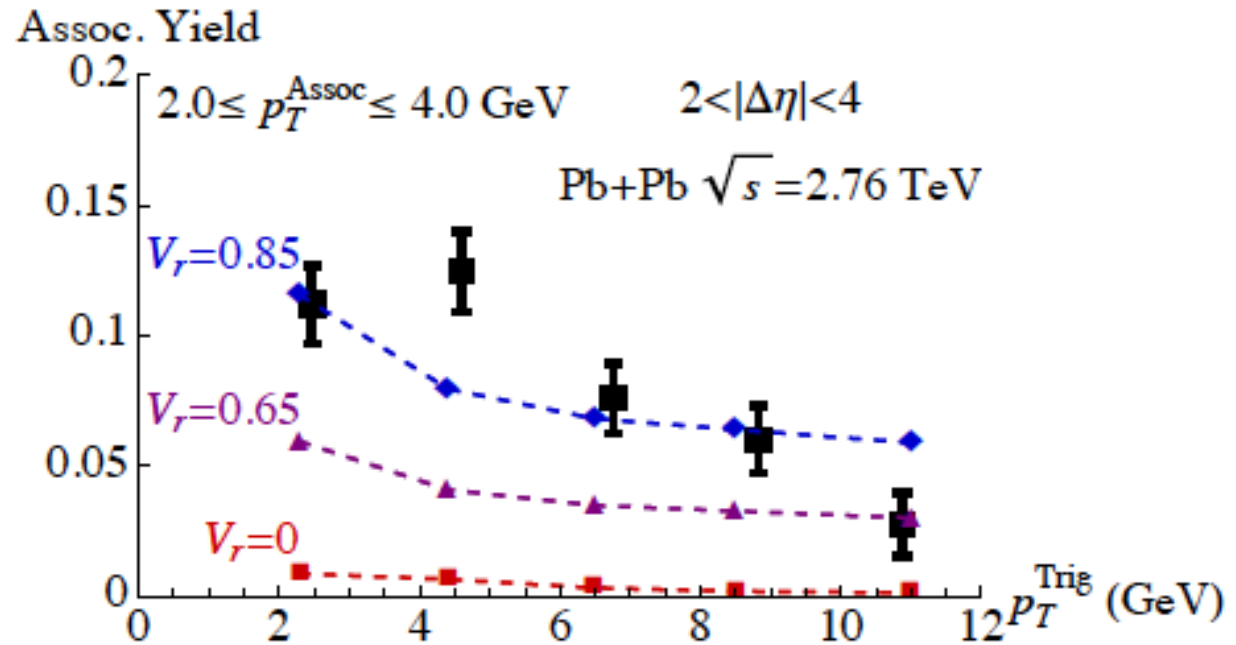
With increasing flow, the pedestal gets collimated

Associated yield reflects the p_T dependence of the Glasma pedestal

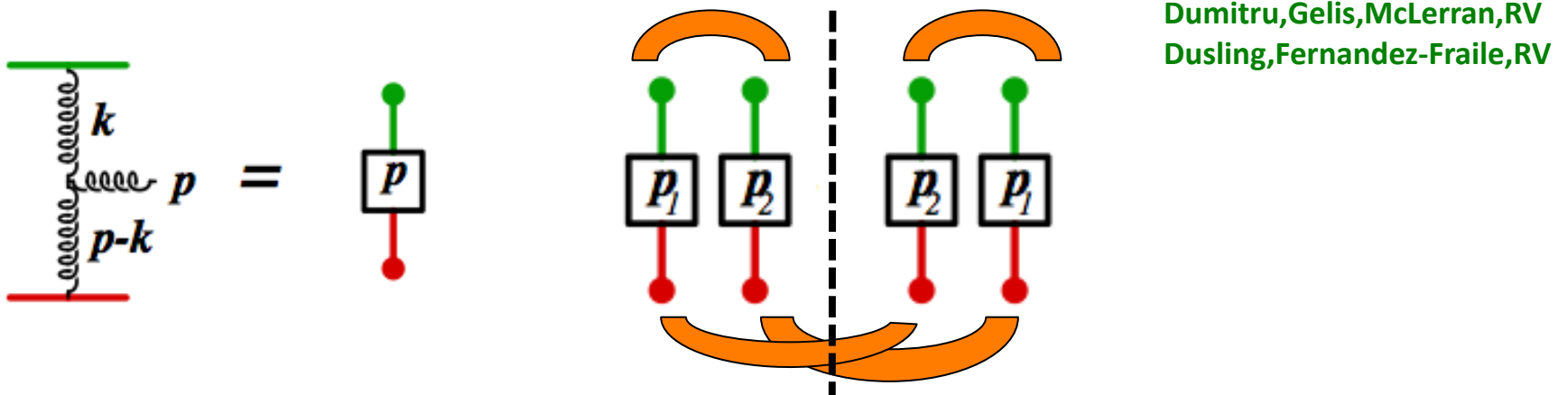
Can accommodate only very small re-scattering / flow contribution

A+A ridge is all flow

Preliminary CMS data



2-particle \rightarrow n-particle correlations

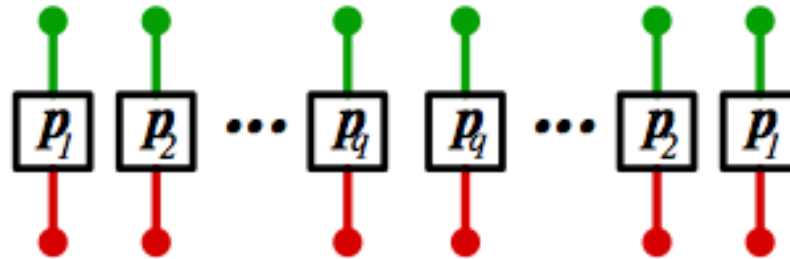


Glasma flux tube picture: two particle correlations
proportional to ratio $1/Q_s^2 / S_T$

Only certain color combinations of “dimers” give leading contributions
...iterating combinatorics for 2, 3, n...gives

2-particle n-particle correlations

Gelis, Lappi, McLerran



Multiplicity distribution: Leading combinatorics of dimers gives the negative binomial distribution

$$P_n^{\text{N.B.}}(\bar{n}, k) = \frac{\Gamma(k + n)}{\Gamma(k)\Gamma(n + 1)} \frac{\bar{n}^n k^k}{(\bar{n} + k)^{n+k}}$$

$$k = \zeta \frac{(N_c^2 - 1) Q_S^2 S_\perp}{2\pi}$$

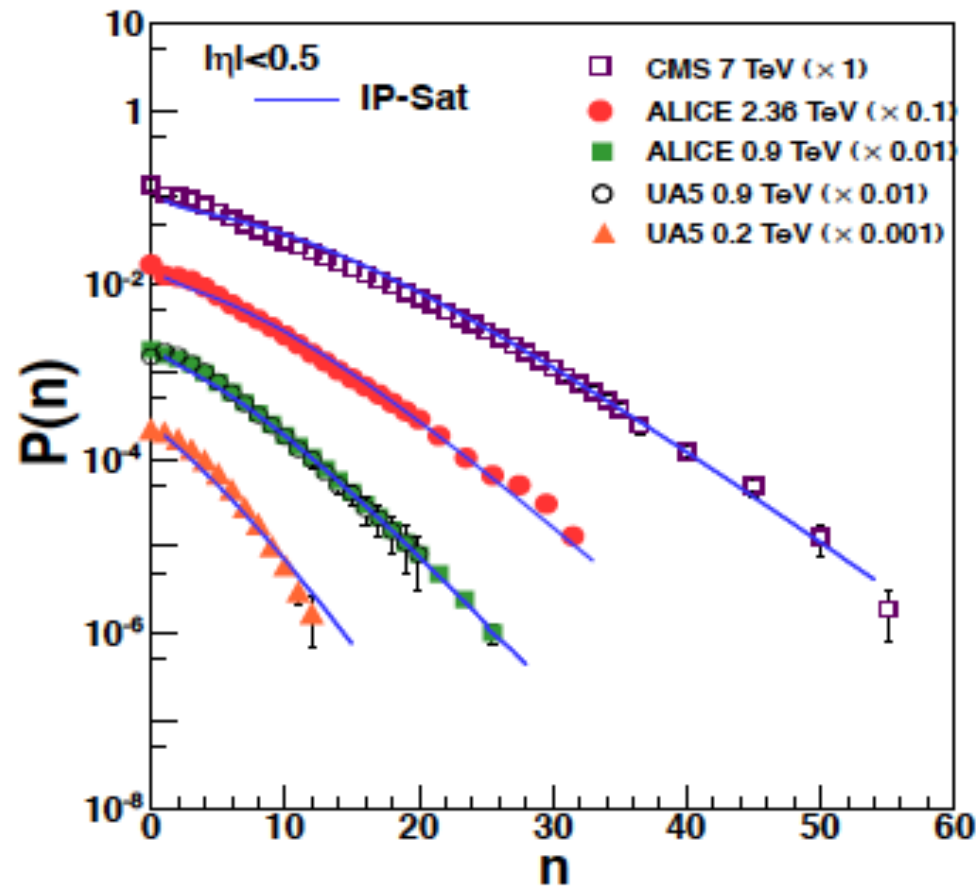
$k = 1$: Bose-Einstein

$k = \infty$: Poisson

Yang-Mills computation shows picture is robust for 2 part. Corr. and gives $\zeta \sim 1/3 - 3/2 \dots O(1)$

Lappi, Srednyak, RV

Convolution of NBDs describes LHC p+p data



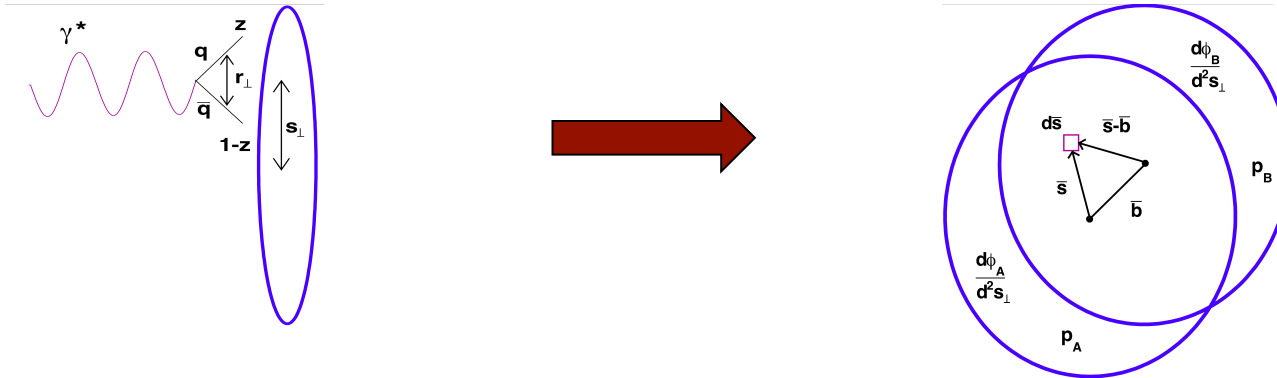
Tribedy, RV
1112.2445

Dynamical quantum fluctuations in energy/# of gluons event-by-event

From nuts to soup: I. constraining initial conditions

First understand e+p and p+p:

Global analysis of HERA data thus far performed only in the IP-Sat, b-CGC and rcBK saturation models - more detailed JIMWLK analysis is desirable and likely



Unintegrated proton gluon dist. from dipole cross-section:

$$\frac{d\phi(x, k_{\perp} | s_{\perp})}{d^2 s_{\perp}} = \frac{k_{\perp}^2 N_c}{4 \alpha_s} \int_0^{\infty} d^2 r_{\perp} e^{ik_{\perp} \cdot r_{\perp}} \left[1 - \frac{1}{2} \frac{d\sigma_{\text{dip.}}^p}{d^2 s_{\perp}}(r_{\perp}, x, s_{\perp}) \right]^2$$

k_{\perp} factorization: compute inclusive dist. of produced gluons at given impact par. :

$$\frac{dN_g(b_{\perp})}{dy d^2 p_{\perp}} = \frac{16 \alpha_s}{\pi C_F} \frac{1}{p_{\perp}^2} \int \frac{d^2 k_{\perp}}{(2\pi)^5} \int d^2 s_{\perp} \frac{d\phi_A(x, k_{\perp} | s_{\perp})}{d^2 s_{\perp}} \frac{d\phi_B(x, p_{\perp} - k_{\perp} | s_{\perp} - b_{\perp})}{d^2 s_{\perp}}$$

The IP-Sat model

Bartels,Golec-Biernat,Kowalski
Kowalski,Teaney
Kowalski,Motyka,Watt

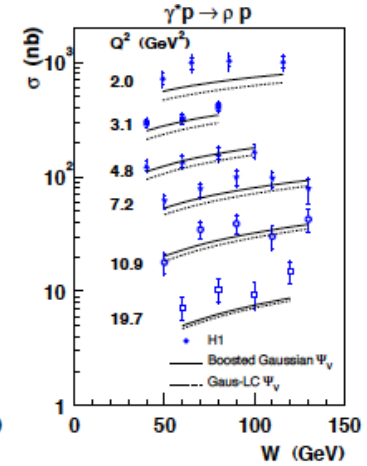
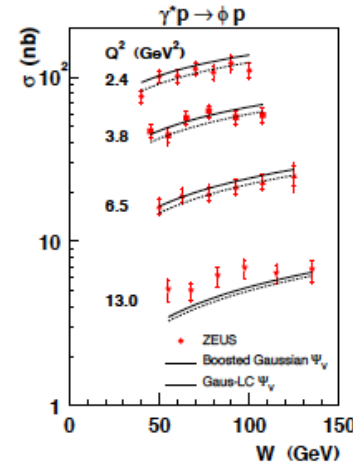
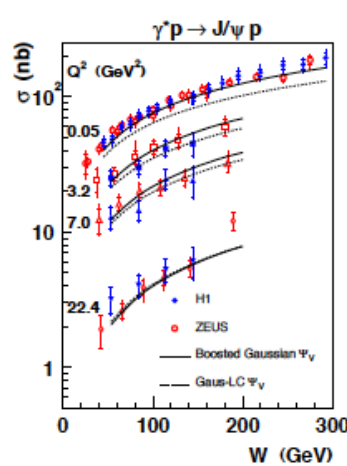
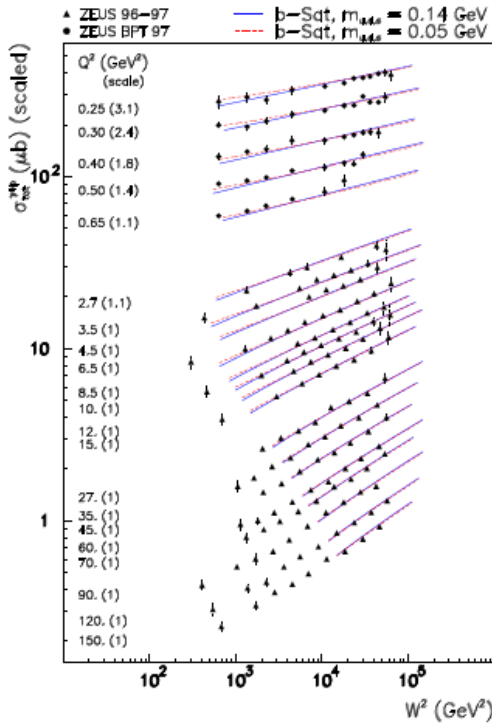
$$\frac{d\sigma_{\text{dip}}^p}{d^2b_{\perp}}(\mathbf{r}_{\perp}, x, \mathbf{b}_{\perp}) = 2\mathcal{N}(\mathbf{r}_{\perp}, x, \mathbf{b}_{\perp}) = 2 \left[1 - \exp \left(-\frac{\pi^2}{2N_c} r_{\perp}^2 \alpha_s(\tilde{\mu}^2) x g(x, \tilde{\mu}^2) T_p(\mathbf{b}_{\perp}) \right) \right]$$

$$\tilde{\mu}^2 = \mu_0^2 + \frac{4}{r_{\perp}^2}$$

MV model extended to small x + impact parameter dependence

$$T_p(b_{\perp}) = e^{-\frac{b_{\perp}^2}{2B_G}}$$

→ Average gluon radius of the proton extracted from HERA diffractive data

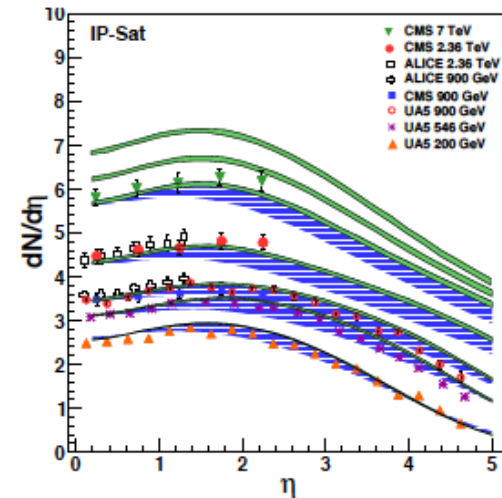
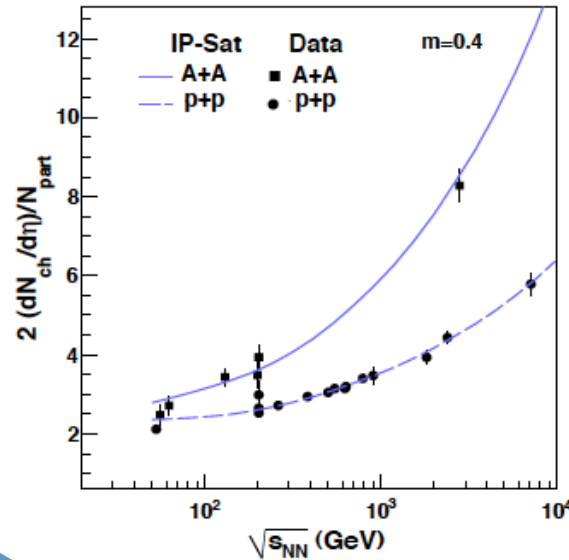
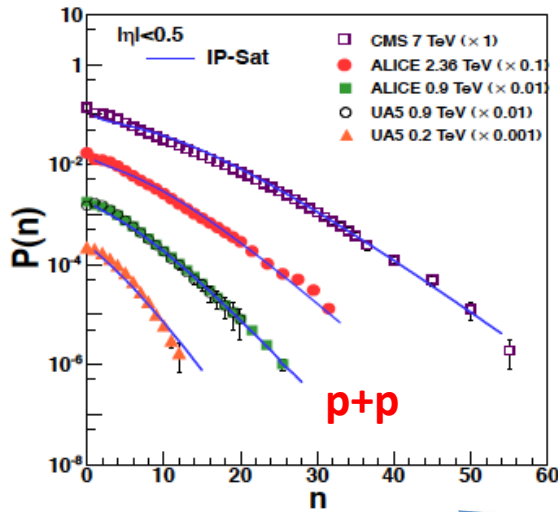


$\chi^2 \sim 1$ fits to HERA inclusive, diffractive and exclusive small x data with few parameters

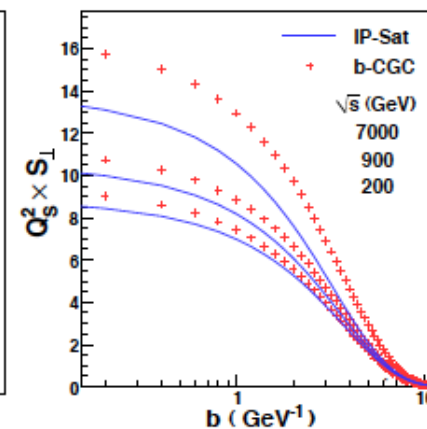
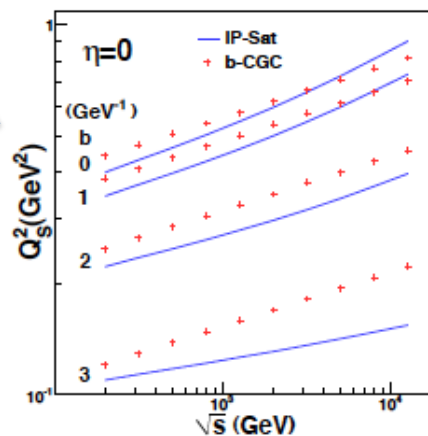
IP-Sat: from HERA to RHIC/LHC

Levin, Rezaiean
Tribedy, RV: 1011.1895,
1112.2445

e+p constrained fits give good description of p+p data

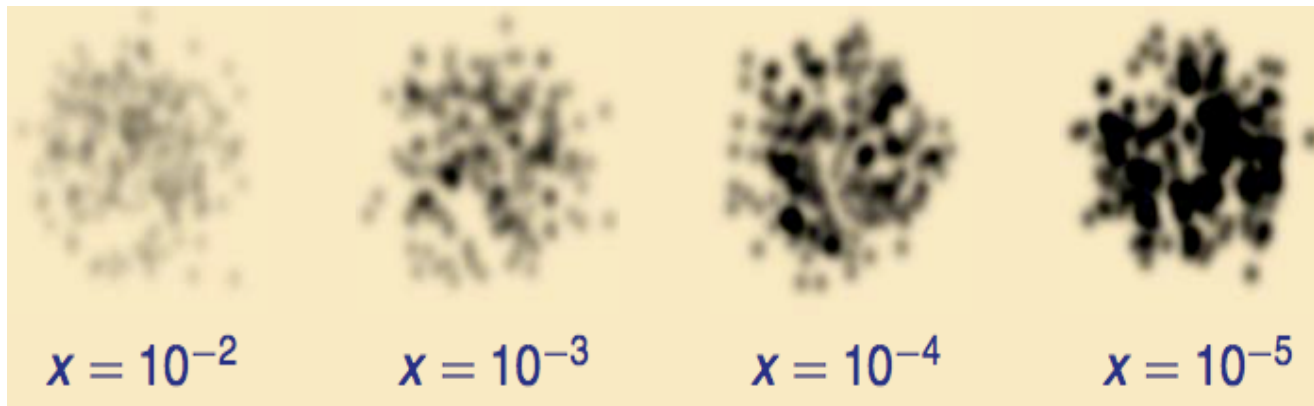
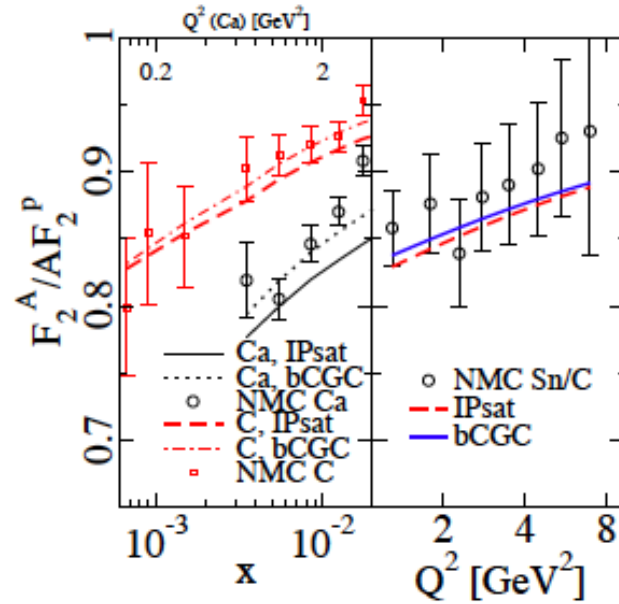


Impact parameter
dependence (constrained by
HERA diffractive data)
important for good agreement
with data



Lumpy nuclei: constrained by (limited) DIS data

Kowalski, Lappi, RV (2008)



From nuts to soup: II. the IP-Glasma model

Schenke, Tribedy, RV:1202.6646, PRL, in press

A. Construct color charge distributions, event-by-event:

- Positions of nucleons sampled from the Woods-Saxon distribution of each nucleus A and B
- IP-Sat provides $Q_S^2(x, b_T)$ for each nucleon – proportional to color charge squared per unit area $g^2\mu_p^2$ (details, see T. Lappi, arXiv:0711.3039)
- Add all $g^2\mu_p^2(x_T)$ to obtain $g^2\mu_A^2(x_T)$ and $g^2\mu_B^2(x_T)$
- Sample $\rho_{A,B}^a$ from local Gaussian distribution for each nucleus:

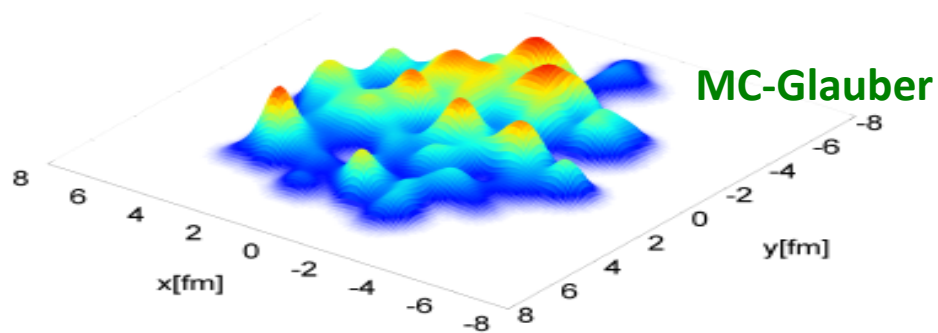
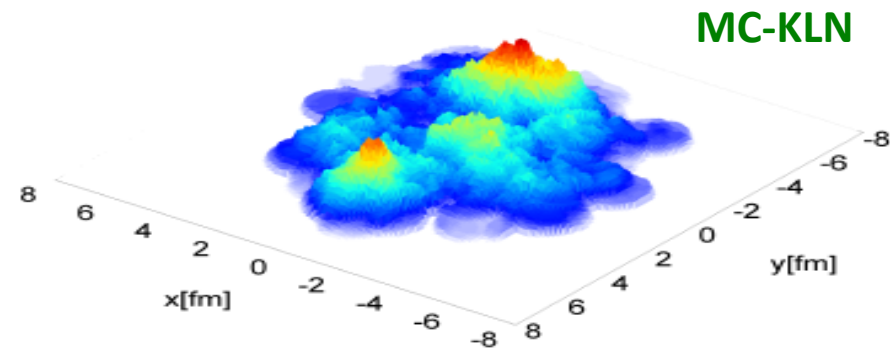
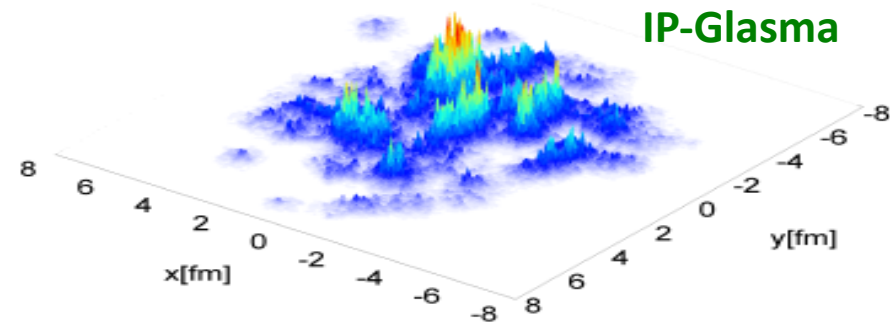
$$\langle \rho_k^a(x_\perp) \rho_l^b(y_\perp) \rangle = \delta_{kl} \delta^{ab} \delta^{(2)}(x_\perp - y_\perp) g^2 \mu_{A,B}^2(x_\perp)$$

This gives the random static source distribution for event-by-event multi-particle production

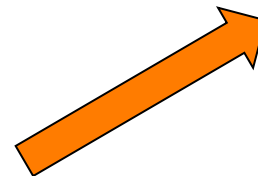
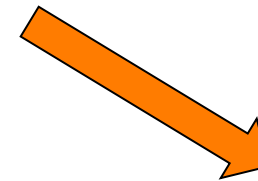
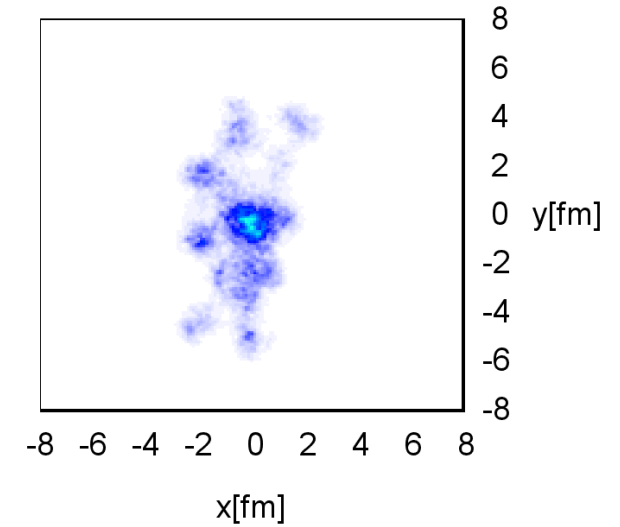
Some “hydro initial conditions” in the literature

- original KLN:
 - uses k_T -factorization
 - $(Q_s^A)^2(\mathbf{x}_\perp) \propto N_{\text{part},A}(\mathbf{x}_\perp)$.
 - Saturation scales are not universal: $N_{\text{part},A}(\mathbf{x}_\perp)$ depends on nucleus B.
 - The energy density ($\epsilon \propto Q_{s,\text{larger}} Q_{s,\text{smaller}}^2$) is suppressed in the edge region along the impact parameter direction \rightarrow larger eccentricity.
- fKLN:
 - uses k_T -factorization
 - Different definition of unintegrated gluon distribution (correct limit: where there is one nucleon at the edge the uGDF is that of one nucleon - not so in KLN)
 - Universal saturation scales in nucleus A and B. (Important at the edges of the nuclei)
- MC-KLN: Monte-Carlo implementation of fKLN with fluctuating positions of the nucleons
- IP-Glasma (CYM):
 - Does not use k_T -factorization (because it is strictly not valid in A+A collisions - at least one source has to be dilute)
 - $Q_s(\mathbf{x}_\perp)$ universal and constrained by HERA data.
 - No utilization of the nucleon-nucleon cross section.
 - Takes into account non-linearities.
 - Includes fluctuations of color charges within a nucleon.

Granularity of initial distributions



Flow

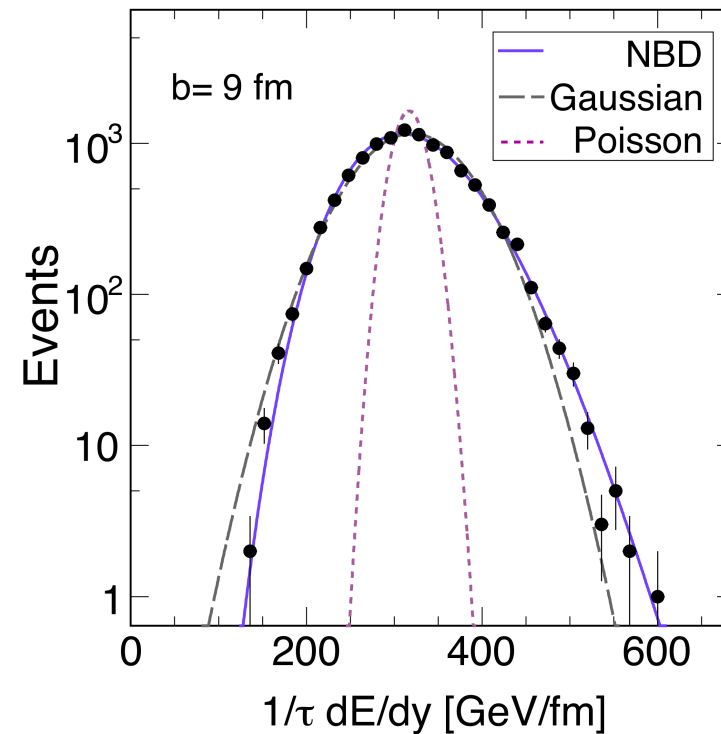
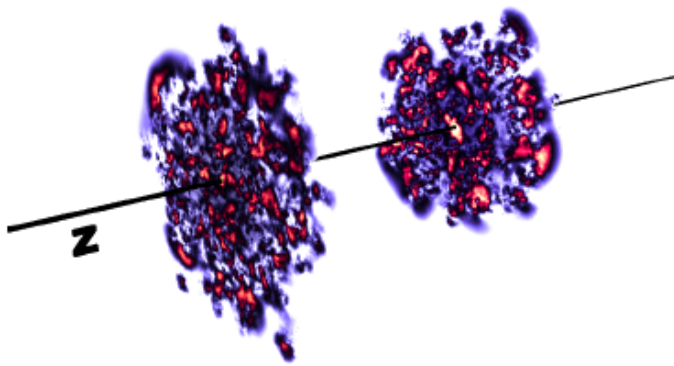


These models do not include KNO/NBD multiplicity fluctuations

Dumitru, Nara

Fluctuating energy distributions from event-by-event solutions of Yang-Mills eqns.

Schenke, Tribedy, RV, arXiv:1202.6646

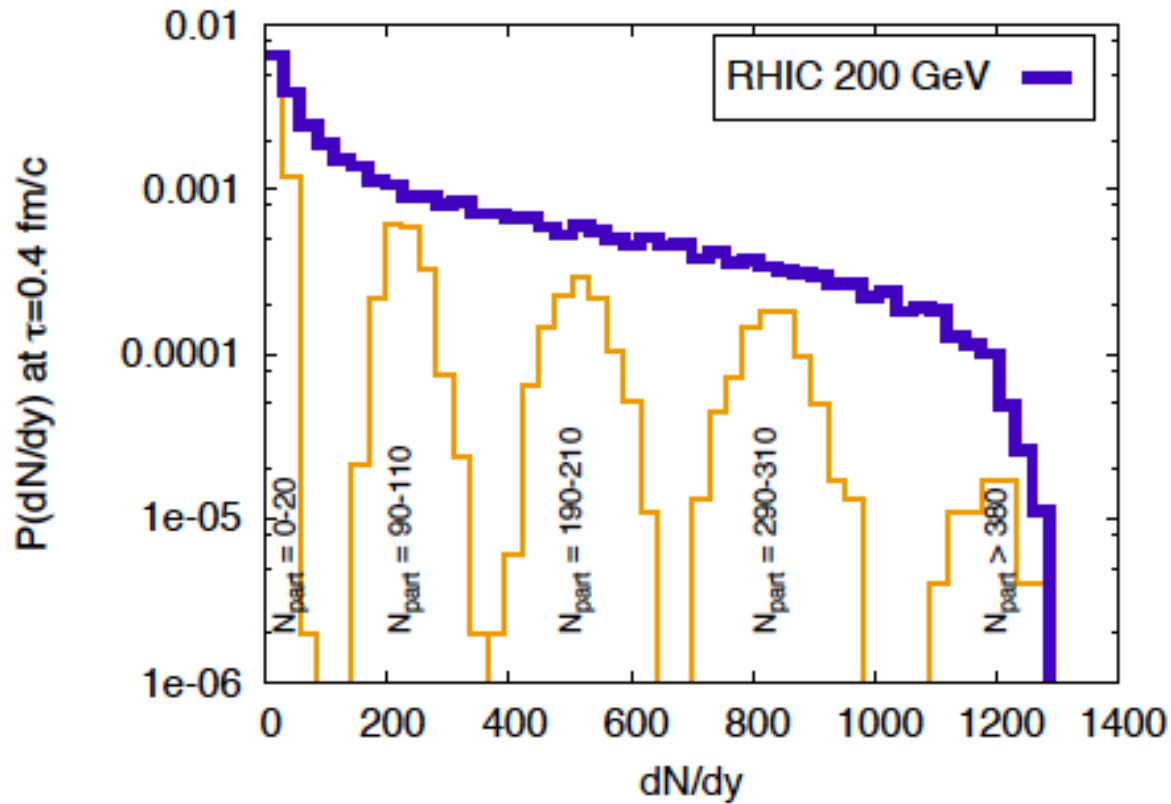


Dynamical quantum fluctuations in energy/# of gluons event-by-event

Gelis, Lappi, McLerran, arXiv: 0905.3234

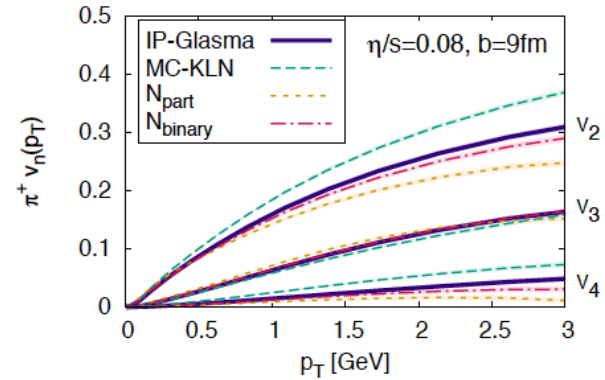
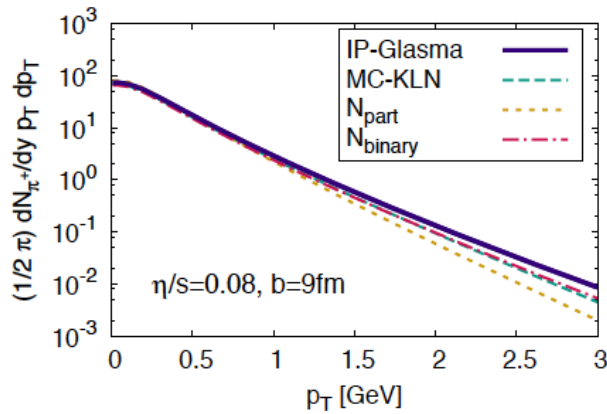
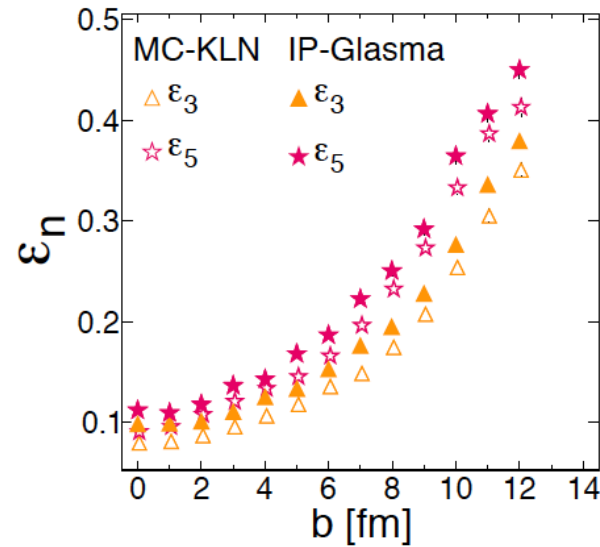
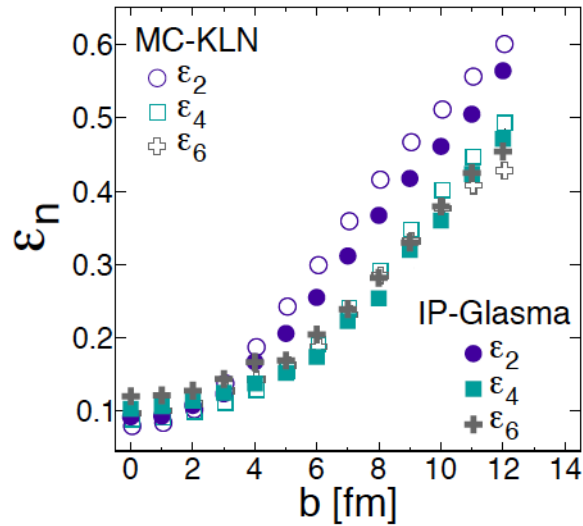
Lappi, Srednyak, RV, arXiv: 0911.2068

Construct nuclear mult. distributions from NBDs



Flow distributions

Schenke, Tribedy, RV, arXiv:1202.6646



First study: may be feasible extract essential physics on how quantum field fluctuations generate flow